

# ATOMIC STRUCTURE

## 2.0 INTRODUCTION

Atom is a Greek word and its meaning is indivisible i.e. an ultimate particle which cannot be further subdivided. John Dalton considered that "all matter are composed of smallest indivisible particle called atom.

### Dalton's Atomic Theory :

This theory is based on law of mass conservation and law of definite proportions. The salient features of this theory are :-

- (1) Each element is composed of extremely small particles called atoms.
- (2) Atoms of a particular element are like but differ from atoms of other element.
- (3) Atom of each element is an ultimate particle and it has a characteristic mass but is structureless
- (4) Atoms are indestructible i.e. they can neither be created nor be destroyed.
- (5) Atoms of different elements take part in chemical reaction to form molecule.

### GOLDEN KEY POINTS

- Particles carrying negative charge were called negatrons by Thomson. The name negatron was changed to 'electron' by Stoney.

In cathode ray experiment, particles (electron) forming the rays have same specific charge ( $e/m$ ) which is independent of the nature of gas and electrode used. It points out that electrons are present in all atoms.

- Mass of electron is  $\frac{1}{1837}$  times that of proton.

- Mass of moving electron =  $\frac{\text{rest mass of electron}}{\sqrt{1-(v/c)^2}}$

(Where  $v$  is the velocity of the electron and  $c$  is the velocity of light.)

When  $v = c \Rightarrow$  mass of electron =  $\infty$  and if  $v > c \Rightarrow$  mass of electron = imaginary

- In anode ray experiment, the particles forming rays have  $e/m$  value that is dependent on the nature of the gas taken in the discharge tube, i.e. +ve particles are different in different gases. Therefore, the mass of the proton can be calculated.

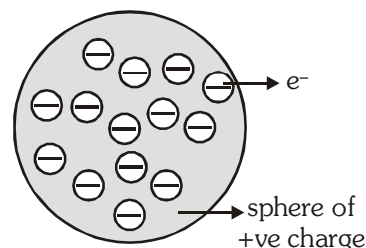
## 2.1 ATOMIC MODELS

### (A) Thomson's Model of Atom [1904]

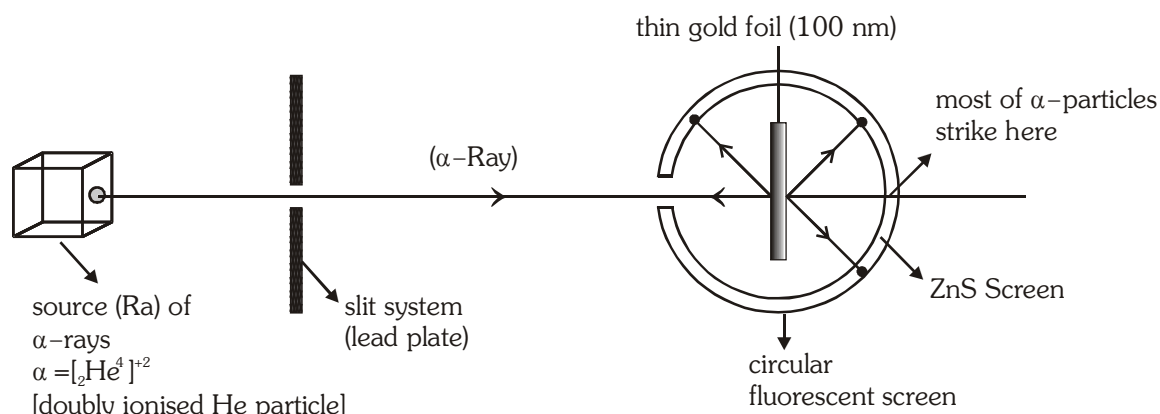
- Thomson was the first to propose a detailed model of the atom.
- Thomson proposed that an atom consists of a uniform sphere of positive charge in which the electrons are distributed more or less uniformly.
- This model of atom is known as "Plum-Pudding model" or "Raisin Pudding Model" or "Water Melon Model".

### Drawbacks :

- An important drawback of this model is that the mass of the atoms is considered to be evenly spread over that atom.
- It is a static model. It does not reflect the movement of electron.
- It couldn't explain the stability of an atom.



## (B) Rutherford's Scattering Experiment



Rutherford observed that -

- Most of the  $\alpha$ -particles passed through the gold foil undeflected.
- A small fraction of the  $\alpha$ -particles were deflected by small angles.
- A very few  $\alpha$ -particles ( $\sim 1$  in 20,000) bounced back, that is, were deflected by nearly  $180^\circ$ .

Following conclusions were drawn from the above observations -

- Since most of the  $\alpha$ -particles went straight through the metal foil undeflected, it means that there must be very large empty space within the atom.
  - Since few of the  $\alpha$ -particles were deflected from their original paths through moderate angles; it was concluded that whole of the +ve charge is concentrated and the space occupied by this positive charge is very small in the atom.
- Diagram illustrating the interaction of  $\alpha$ -particles with the nucleus:

  - $\alpha$ -particles
  - Nucleus
  - Undeflected  $\alpha$ -particles
  - Slightly deflected  $\alpha$ -particles
  - Largely deflected  $\alpha$ -particles
- When  $\alpha$ -particles come closer to this point, they suffer a force of repulsion and deviate from their paths.
  - The positively charged heavy mass which occupies only a small volume in an atom is called **nucleus**. It is supposed to be present at the centre of the atom.
  - A very few of the  $\alpha$ -particles suffered strong deflections or even returned on their path indicating that the nucleus is rigid and  $\alpha$ -particles recoil due to direct collision with the heavy positively charged mass.

## (C) RUTHERFORD'S ATOMIC MODEL

On the basis of scattering experiments, Rutherford proposed model of the atom, which is known as nuclear atomic model. According to this model -

- An atom consists of a heavy positively charged nucleus where all the protons and neutrons are present. Protons & neutrons are collectively referred to as nucleons. Almost whole of the mass of the atom is contributed by these nucleons. The magnitude of the +ve charge on the nucleus is different for different atoms.
- The volume of the nucleus is very small and is only a minute fraction of the total volume of the atom. Nucleus has a diameter of the order of  $10^{-12}$  to  $10^{-13}$  cm and the atom has a diameter of the order of  $10^{-8}$  cm.

$$\frac{D_A}{D_N} = \frac{\text{Diameter of the atom}}{\text{Diameter of the nucleus}} = \frac{10^{-8}}{10^{-13}} = 10^5, \quad D_A = 10^5 D_N$$

Thus diameter (size) of the atom is  $10^5$  times the diameter of the nucleus.

- The radius of a nucleus is proportional to the cube root of the number of nucleons within it.

$$R \propto A^{1/3} \Rightarrow R = R_0 A^{1/3}$$

Where  $R_0 = 1.33 \times 10^{-13}$  cm (a constant) and  $A$  = mass number ( $p + n$ ) and  $R$  = radius of the nucleus.

$$R = 1.33 \times 10^{-13} \times A^{1/3} \text{ cm}$$



- (iii) There is an empty space around the nucleus called extra nuclear part. In this part electrons are present. The number of electrons in an atom is always equal to number of protons present in the nucleus. As the nuclear part of atom is responsible for the mass of the atom, the extra nuclear part is responsible for its volume.

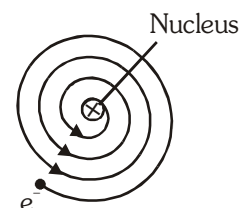
The volume of the atom is about  $10^{15}$  times the volume of the nucleus.

$$\frac{\text{Volume of the atom}}{\text{Volume of the nucleus}} = \frac{(10^{-8})^3}{(10^{-13})^3} = 10^{15}$$

- (iv) Electrons revolve around the nucleus in closed orbits with high speeds. The centrifugal force acting on the revolving electron is being counter balanced by the force of attraction between the electrons and the nucleus.
- This model was similar to the solar system, the nucleus representing the sun and revolving electrons as planets.

### Drawbacks of rutherford model -

- (i) This theory could not explain the stability of atom. According to Maxwell, electron loose its energy continuously in the form of electromagnetic radiations. As a result of this, the  $e^-$  should loose energy at every turn and move closer and closer to the nucleus following a spiral path. The ultimate result will be that it will fall into the nucleus, thereby making the atom unstable.
- (ii) If the electrons loose energy continuously, the observed spectrum should be continuous but the actual observed spectrum consists of well defined lines of definite frequencies. Hence, the loss of energy by electron is not continuous in an atom.



## 2.2 ATOMIC NUMBER AND MASS NUMBER

### (a) Atomic Number

It is represented by Z. The number of protons present in the nucleus is called atomic number of an element.

For neutral atom : Number of electrons = Number of protons

For an ion : Number of electrons =  $Z - (\text{charge on ion})$

$Z =$  number of protons only

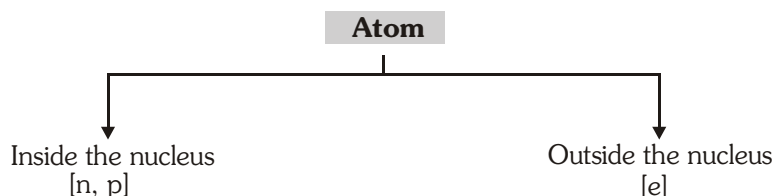
### (b) Mass Number

It is represented by capital A. The sum of number of neutrons and protons is called the mass number of the element. It is also known as number of nucleons because neutrons & protons are present in nucleus.

**Formula :**  $A = \text{number of protons} + \text{number of neutrons}$

Number of neutrons =  $A - Z$

**Note :** A is always a whole number.



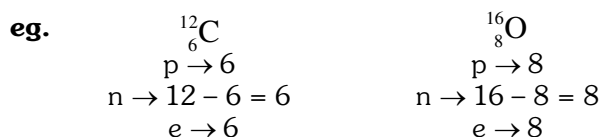
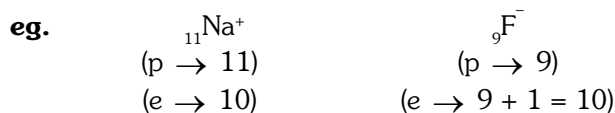
An atom of the element is represented by  ${}^A_ZX$

Where, X = Symbol of element

Z = Atomic number = no. of protons = no. of electrons (If atom is neutral)

A = Mass number = no. of neutrons + Atomic no.

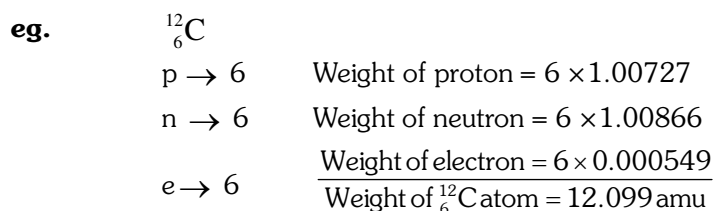




**Mass no. [A] and atomic weight** (amu= atomic mass unit)

Mass of Proton ( $m_p$ )	Mass of Neutron ( $m_n$ )	Mass of Electron ( $m_e$ )
$1.672 \times 10^{-27}$ kg	$1.675 \times 10^{-27}$ kg	$9.1 \times 10^{-31}$ kg
$1.672 \times 10^{-24}$ g	$1.675 \times 10^{-24}$ g	$9.1 \times 10^{-28}$ g
1.00727 amu	1.00866 amu	0.000549 amu

**Method for Analysis of atomic weight  $\rightarrow$**

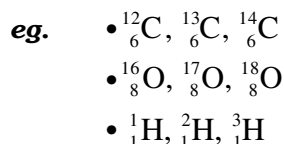


Mass no. of  ${}_{6}^{12}\text{C}$  atom = 12 [p and n]

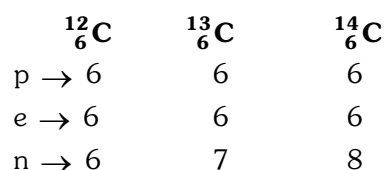
**Note :** Mass no. of atom is always a whole no. but atomic weight may be in decimal.

## 2.3 SOME IMPORTANT DEFINITIONS

(a) **Isotopes :** They are atoms of a given element which have the same atomic number but differ in their mass number.

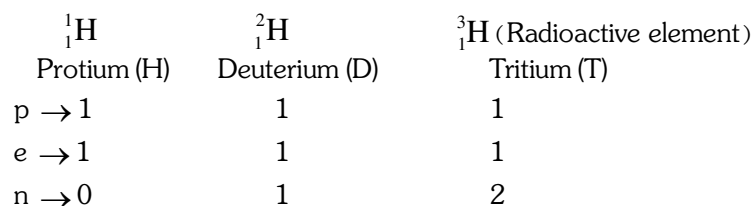


**Explanation 1:**



[**Note :** Isotopes have the same number of protons but differ in the number of neutrons in the nucleus]

**Explanation 2:**



- Neutron is not available in Protium
- No. of Nucleons = No. of Neutrons + No. of Protons  
 $= n + p$



**Atomic Weight :** The atomic weight of an element is the average of mass of all the isotopes of that element.

- If an element have three isotopes  $y_1$ ,  $y_2$  and  $y_3$  and their isotopic weights are  $w_1$ ,  $w_2$ ,  $w_3$  and their percentage/possibility/probability/ratio of occurrence in nature are  $x_1$ ,  $x_2$ ,  $x_3$  respectively, then the average atomic weight of element is

$$\text{Average atomic weight} = \frac{w_1x_1 + w_2x_2 + w_3x_3}{x_1 + x_2 + x_3}$$

<b>eg.</b>	$^{35}\text{Cl}$	$^{37}\text{Cl}$
Probability	75%	25%
ratio	3	1

$$\text{Average atomic weight} = \frac{35 \times 3 + 37 \times 1}{3 + 1} = \frac{142}{4} = 35.5$$

**(b) Isobars**

Isobars are the atoms of different element which have the same mass number but different atomic number i.e they have different number of electrons, protons & neutrons but sum of number of neutrons & protons remains same.

<b>Ex.1</b>	$^3_1\text{H}$	$^3_2\text{He}$	<b>Ex.2</b>	$^{40}_{19}\text{K}$	$^{40}_{20}\text{Ca}$
	p = 1	p = 2		p = 19	p = 20
	e = 1	e = 2		e = 19	e = 20
	n = 2	n = 1		n = 21	n = 20
	p + n = 3	p + n = 3		n + p = 40	n + p = 40

**(c) Isodiaphers**

They are the atoms of different element which have the same difference of the number of Neutrons & protons.

<b>Ex.1</b>	$^{11}_5\text{B}$	$^{13}_6\text{C}$	<b>Ex.2</b>	$^{15}_7\text{N}$	$^{19}_9\text{F}$
	p = 5	p = 6		p = 7	p = 9
	e = 5	e = 6		e = 7	e = 9
	n = 6	n = 7		n = 8	n = 10
	n - p = 1	n - p = 1		n - p = 1	n - p = 1

**(d) Isotones/Isoneutronic Species/Isotonic**

They are the atoms of different element which have the same number of neutrons.

<b>Ex.1</b>	$^3_1\text{H}$	$^4_2\text{He}$	<b>Ex. 2</b>	$^{39}_{19}\text{K}$	$^{40}_{20}\text{Ca}$
	p = 1	p = 2		p = 19	p = 20
	e = 1	e = 2		e = 19	e = 20
	n = 2	n = 2		n = 20	n = 20

**(e) Isosters**

They are the molecules which have the same number of atoms & electrons.

<b>Ex.1</b>	$\text{CO}_2$	$\text{N}_2\text{O}$	<b>Ex.2</b>	$\text{CaO}$	$\text{KF}$
Atoms	= 1 + 2 = 3	Atoms = 2 + 1 = 3	Atoms = 2	Atoms = 2	Atoms = 2
Electrons	= 6 + 8 × 2 = 22 e	Electrons = 7 × 2 + 8 = 22e	Electrons = 20 + 8 = 28 e	Electrons = 19 + 9 = 28 e	Electrons = 19 + 9 = 28 e

**(f) Isoelectronic Species**

They are the atoms, molecules or ions which have the same number of electrons.

<b>Ex.1</b>	$\text{Cl}^-$	$\text{Ar}$
	18 e	18 e
<b>Ex.2</b>	$\text{H}_2\text{O}$	$\text{NH}_3$
	(2 + 8)=10 e	(7 + 3) = 10 e
<b>Ex.3</b>	$\text{BF}_3$	$\text{SO}_2$
	(5 + 9 × 3)=32 e	(16 + 8 × 2)=32 e



## GOLDEN KEY POINTS

- Isotopes have same chemical property but different physical property.
- Isotopes do not have the same value of  $e/m$ .
- Isobars do not have the same chemical & physical property.
- Isobars do not have the same value of  $e/m$
- For isotones,  $A_1 - Z_1 = A_2 - Z_2$
- For isodiaphers,  $A_1 - 2Z_1 = A_2 - 2Z_2$

## Illustrations

**Illustration 1.** If the mass of neutron is doubled & mass of electron is halved then find out the new atomic mass of  ${}^{12}_6\text{C}$  and the percent by which it is increased.

**Solution**      **Step-1**       ${}^{12}_6\text{C} \rightarrow$        $e = 6$

$$\left. \begin{array}{l} p = 6 = 6 \text{ amu} \\ n = 6 = 6 \text{ amu} \end{array} \right\} = 12 \text{ amu}$$

If the mass of neutron is doubled and mass of electron is halved then,

$$\left. \begin{array}{l} n = 12 \text{ amu} \\ p = 6 \text{ amu} \end{array} \right\} = 18 \text{ amu}$$

**Note :** mass of electron is negligible, so it is not considered in atomic mass.

**Step-2**      % Increment =  $\frac{\text{Final mass} - \text{Initial mass}}{\text{Initial mass}} \times 100 = \frac{18 - 12}{12} \times 100 = 50\%$

**Illustration 2.** If mass of neutron is doubled, mass of proton is halved and mass of electron is doubled then find out the new atomic weight of  ${}^{12}_6\text{C}$ .

**Solution**      **Step-1**       ${}^{12}_6\text{C} \rightarrow$        $p = 6$

$$\left. \begin{array}{l} n = 6 \\ \end{array} \right\} = 12 \text{ amu}$$

If mass of neutron is doubled, mass of proton is halved and mass of electron is doubled, then new atomic mass will be :

$$\left. \begin{array}{l} n = 12 \text{ amu} \\ p = 3 \text{ amu} \end{array} \right\} = 15 \text{ amu}$$

**Step-2**      % Increment =  $\frac{\text{Final mass} - \text{Initial mass}}{\text{Initial mass}} \times 100 = \frac{15 - 12}{12} \times 100 = 25\%$

**Illustration 3.** If no. of protons in  $\text{X}^{-2}$  is 16. then no. of electrons in  $\text{X}^{+2}$  will be—  
 (1) 14                                  (2) 16                                  (3) 18                                  (4) None

**Solution**       $\therefore$  No. of protons in  $\text{X}^{-2}$  is = 16  
 $\therefore$  No. of electrons in  $\text{X}^{+2}$  is = 14

**Illustration 4.** Assuming that atomic weight of  ${}^{12}\text{C}$  is 150 unit from atomic table, then according to this assumption, the weight of  ${}^{16}\text{O}$  will be :-

**Solution**       $\therefore 12 \text{ amu} = 150$

$$\therefore 1 \text{ amu} = \frac{150}{12}$$

$$\therefore 16 \text{ amu} = \frac{150}{12} \times 16 = 200 \text{ Unit}$$



**Illustration 5.** An element have three isotopes and their isotopic weights are 11, 12, 13 unit and their percentage of occurrence in nature is 85, 10, 5 respectively, then calculate the average atomic weight of element.

**Solution** Average Atomic weight =  $\frac{11 \times 85 + 12 \times 10 + 13 \times 5}{85 + 10 + 5} = \frac{935 + 120 + 65}{100}$

Average weight =  $\frac{1120}{100} = 11.2$

**Illustration 6.** Average atomic weight of an element M is 51.7. If two isotopes of M are  $^{50}\text{M}$  and  $^{52}\text{M}$ , then calculate the percentage of occurrence of  $^{50}\text{M}$  in nature.

**Solution**

$$\begin{array}{l} {}^{50}\text{M} \quad \quad {}^{52}\text{M} \\ x_1 \quad + \quad x_2 = 100 \\ x_2 = (100 - x_1) \end{array}$$

$$\text{average atomic weight} = \frac{w_1x_1 + w_2x_2}{x_1 + x_2} = 51.7 = \frac{50 \times x_1 + 52 \times x_2}{x_1 + x_2}$$

$$51.7 = \frac{50x_1 + 52(100 - x_1)}{x_1 + (100 - x_1)}$$

$$5170 = 50x_1 + 5200 - 52x_1$$

$$5170 = -2x_1 + 5200$$

$$2x_1 = 30$$

$$x_1 = 15$$

$${}^{50}\text{M} = 15\% \quad {}^{52}\text{M} = 85\%$$

### BEGINNER'S BOX-1

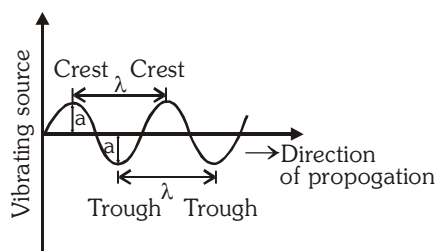
- Which of the following statements is incorrect for anode rays?
  - (1) They are deflected by electric and magnetic fields.
  - (2) Their  $e/m$  ratio depends on the gas in the discharge tube used to produce the anode rays.
  - (3) The  $e/m$  ratio of anode rays is constant.
  - (4) They are produced by the ionisation of the gas in the discharge tube.
- Which of the following pairs have identical value of  $e/m$ ?
  - (1) A proton and a neutron
  - (2) A proton and deuteron
  - (3) Deuteron and an  $\alpha$  - particle
  - (4) An electron and  $\gamma$  - rays
- Rutherford's  $\alpha$  - particle scattering experiments led to the conclusion that
  - (1) mass and energy are related together
  - (2) the mass and the positive charge of an atom are concentrated in the nucleus
  - (3) neutrons are present in the nucleus
  - (4) atoms are electrically neutral
- The radius of nucleus  ${}_{13}^{27}\text{Al}$  will be
  - (1)  $1.2 \times 10^{-15} \text{ m}$
  - (2)  $2.7 \times 10^{-15} \text{ m}$
  - (3)  $10.8 \times 10^{-15} \text{ m}$
  - (4)  $4 \times 10^{-15} \text{ m}$
- Which of the following elements has maximum density of nucleus.
  - (1)  ${}_{14}^{30}\text{SO}$
  - (2)  ${}_{15}^{31}\text{P}$
  - (3)  ${}_{8}^{16}\text{O}$
  - (4) All have same density
- Select iso electronic set :-
  - (a)  $\text{Na}^+, \text{H}_3\text{O}^+, \text{NH}_4^+$
  - (b)  $\text{CO}_3^{2-}, \text{NO}_3^-, \text{H}_2\text{CO}_3$
  - (c)  $\text{P}^{3-}, \text{HCl}, \text{C}_2\text{H}_5^-, \text{PH}_3$
  - (d)  $\text{F}^-, \text{Ne}, \text{Na}^+$
  - (1) a, b, d
  - (2) b, c, d
  - (3) a, b, c
  - (4) a, b, c, d
- If the table of atomic masses were established with the oxygen atom and assigned value of 100, then the mass of carbon atom would be, approximately:-
  - (1) 24
  - (2) 75
  - (3) 50
  - (4) 112



## 2.4 ELECTROMAGNETIC WAVES (EM WAVES) OR RADIANT ENERGY

According to this theory, the energy is transmitted from one body to another in the form of waves and these waves travel in the space with the same speed as light ( $3 \times 10^8$  m/s). These waves are known as Electro magnetic waves or radiant energy. **Ex :** Radio waves, micro waves, Infra red rays, visible rays, ultraviolet rays, X-rays, gamma rays.

- The radiant energy do not need any medium for propogation.
- The radiant energy have electric and magnetic fields and travel at right angle to these fields.
- The upper most point of the wave is called crest and the lower most point is called trough.



Some of the terms employed in dealing with the waves are described below.

- (1) Wavelength ( $\lambda$ ) (Lambda) :** It is defined as the distance between two nearest crest or trough.

It is measured in terms of Å (Angstrom), pm (picometre), nm (nanometer), cm (centimetre), m (metre)

$$1\text{Å} = 10^{-10}\text{ m}, \quad 1\text{ pm} = 10^{-12}\text{ m}, \quad 1\text{ nm} = 10^{-9}\text{ m}, \quad 1\text{ cm} = 10^{-2}\text{ m}$$

- (2) Wave number ( $\bar{\nu}$ ) (nu bar) :** It is the reciprocal of the wavelength, that is number of waves present in

unit length

$$\bar{\nu} = \frac{1}{\lambda}$$

It is measured in terms of  $\text{cm}^{-1}$ ,  $\text{m}^{-1}$  etc.

- (3) Frequency ( $\nu$ ) (nu) :** Frequency of a wave is defined as the number of waves which pass through a point in 1 s. It is measured in terms of Hertz (Hz),  $\text{s}^{-1}$  or cycle/s(cps) (1 Hertz =  $1\text{ s}^{-1}$ )

- (4) Time period (T) :** Time taken by a wave to pass through one point.  $T = \frac{1}{\nu} \text{ second}$

- (5) Velocity (c) :** Velocity of a wave is defined as distance covered by a wave in 1 second

$$c = \lambda / T = \lambda \nu \text{ or } \nu = c / \lambda \text{ or } c = \nu (\text{s}^{-1}) \times \lambda (\text{m}) \text{ or } c = \nu \lambda (\text{m s}^{-1})$$

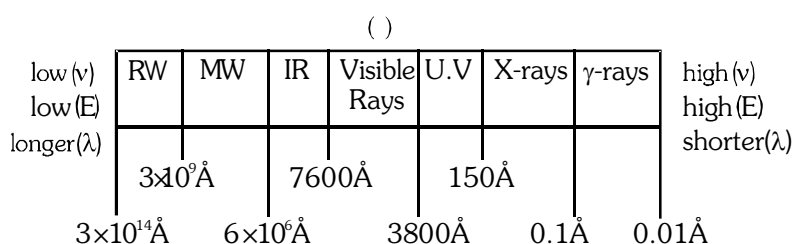
Since c is constants i.e. frequency is inversely propotional to  $\lambda$

- (6) Amplitude (a) :** The amplitude of a wave is defined as the height of crust or depth of trough.

**Important note :**  $\nu = \frac{c}{\lambda} = c\bar{\nu} \quad \left( \bar{\nu} = \frac{1}{\lambda} \right)$

### Electromagnetic spectrum or EM spectrum :

The arrangement obtained by arranging various types of EM waves in order of their increasing frequency or decreasing wave length is called as EM SPECTRUM





## Illustrations

**Illustration 7.** The Vividh Bharti station of All India Radio broadcasts on a frequency of 1368 kilo hertz. Calculate the wavelength of the electromagnetic waves emitted by the transmitter.

**Solution** As we know velocity of light ( $c$ ) =  $3 \times 10^8$  m/s

Given  $\nu$  (frequency) = 1368 kHz =  $1368 \times 10^3$  Hz =  $1368 \times 10^3$  s<sup>-1</sup>

$$\therefore \lambda = \frac{c}{\nu} \quad \therefore \lambda = \frac{3 \times 10^8 \text{ ms}^{-1}}{1368 \times 10^3 \text{ s}^{-1}} = 219.3 \text{ m}$$

**Illustration 8.** Calculate  $\bar{\nu}$  in cm<sup>-1</sup> and  $\nu$  of yellow radiation having a wavelength of 5800 Å

**Solution** As we know  $\bar{\nu} = \frac{1}{\lambda} = \frac{1}{5800 \text{ Å}} = \frac{1}{5800 \times 10^{-8} \text{ cm}} = \frac{10^8}{5800} \text{ cm}^{-1} = 17241.37 \text{ cm}^{-1}$

$$\nu = c \bar{\nu} = 3 \times 10^{10} \text{ cm s}^{-1} \times 1.7 \times 10^4 \text{ cm}^{-1} = 3 \times 1.7 \times 10^{14} = 5.1 \times 10^{14} \text{ s}^{-1}$$

**Illustration 9.** A particular radiostation broadcast at a frequency of 1120 kilo hertz. Another radio station broadcast at a frequency of 98.7 mega hertz. What are the wavelength of radiations from each station.

**Solution** Station 1<sup>st</sup>  $\lambda = \frac{c}{\nu} = \frac{3 \times 10^8 \text{ ms}^{-1}}{1120 \times 10^3 \text{ s}^{-1}} = 267.86 \text{ m}$

$$\text{Station 2}^{\text{nd}} \quad \lambda = \frac{c}{\nu} = \frac{3 \times 10^8 \text{ ms}^{-1}}{98.7 \times 10^6 \text{ s}^{-1}} = 3.0395 \text{ m}$$

**Illustration 10.** How long would it take a radio wave of frequency  $6 \times 10^3$  s<sup>-1</sup> to travel from mars to earth, that is a distance of  $8 \times 10^7$  km ?

**Solution** Distance to be travelled from mars to earth =  $8 \times 10^7$  km =  $8 \times 10^{10}$  m

$\therefore$  Velocity of EM waves =  $3 \times 10^8$  m/s

$$\therefore \text{Time} = \frac{\text{Distance}}{\text{Velocity}} = \frac{8 \times 10^{10} \text{ m}}{3 \times 10^8 \text{ m/s}} = 2.66 \times 10^2 \text{ s} = 4 \text{ min } 26 \text{ s}$$

## 2.5 PLANCK'S QUANTUM THEORY

According to planck's quantum theory :

- (1) The radiant energy emitted or absorbed by a body not continuously but discontinuously in the form of small discrete packets of energy and these packets are called quantum.
- (2) In case of light, the smallest packet of energy is called as 'photon' but in general case the smallest packet of energy is called as quantum.
- (3) The energy of each quantum is directly proportional to frequency of the radiation i.e.

$$E \propto \nu \quad \Rightarrow \quad E = h\nu \quad \text{or} \quad E = \frac{hc}{\lambda} \left\{ \because \nu = \frac{c}{\lambda} \right\}$$

$h$  is proportionality constant or Planck's constant

$$h = 6.626 \times 10^{-37} \text{ kJ s} \quad \text{or} \quad 6.626 \times 10^{-34} \text{ J s} \quad \text{or} \quad 6.626 \times 10^{-27} \text{ erg s}$$

- (4) Total amount of energy transmitted from one body to another will be some integral multiple of energy of

a quantum.

$$E = nh\nu = \frac{nhc}{\lambda} = nhc\bar{\nu}$$

where  $n$  = Positive integer

= Number of quanta



## Illustrations

**Illustration 11.** Calculate the energy of a photon of sodium light of wave length  $5.862 \times 10^{-16} \text{ m}$  in joule.

**Soluiton**  $\lambda = 5.862 \times 10^{-16} \text{ m}, \quad c = 3 \times 10^8 \text{ m s}^{-1}$

$$E = nh\nu \quad \text{or} \quad \frac{nhc}{\lambda} \quad \{ \because n = 1 \}$$

$$\therefore E = \frac{hc}{\lambda} = \frac{1 \times 6.6 \times 10^{-34} \text{ J s} \times 3 \times 10^8 \text{ ms}^{-1}}{5.862 \times 10^{-16} \text{ m}} = \frac{6.6 \times 3}{5.862} \times 10^{-10} \text{ J} = 3.38 \times 10^{-10} \text{ J}$$

**Illustration 12.** Calculate the frequency & energy of a photon of wave length  $4000 \text{ \AA}$ .

**Soluiton** (a) Calculation of frequency :  $\lambda = 4000 \text{ \AA} = 4000 \times 10^{-10} \text{ m}$

$$\therefore \nu = \frac{c}{\lambda} = \frac{3 \times 10^8 \text{ m/s}}{4 \times 10^{-7} \text{ m}} = 0.75 \times 10^{15} \text{ s}^{-1} = 7.5 \times 10^{14} \text{ s}^{-1}$$

(b) Calculation of energy :

$$E = h\nu = 6.626 \times 10^{-34} \text{ joule second} \times 7.5 \times 10^{14} \text{ s}^{-1} = 4.96 \times 10^{-19} \text{ joule}$$

**Illustration 13.** Calculate the  $\lambda$  and frequency of a photon having an energy of 2 electron volt

**Soluiton**  $\therefore 1\text{eV} = 1.602 \times 10^{-19} \text{ J} \therefore 2\text{eV} = 3.204 \times 10^{-19} \text{ J} = E$

$$\begin{aligned} \text{(a) Calculation of wavelength } (\lambda) : E &= \frac{hc}{\lambda} \text{ or } \lambda = \frac{hc}{E} = \frac{6.626 \times 10^{-34} \text{ Js} \times 3 \times 10^8 \text{ ms}^{-1}}{3.204 \times 10^{-19} \text{ J}} \\ &= 6.204 \times 10^{-7} \text{ m} \end{aligned}$$

$$\text{(b) Calculation of frequency } (\nu) : \nu = \frac{c}{\lambda} = \frac{3 \times 10^8 \text{ ms}^{-1}}{6.204 \times 10^{-7} \text{ m}} = 0.49 \times 10^{15} \text{ s}^{-1} = 4.9 \times 10^{14} \text{ s}^{-1}$$

**Illustration 14.** Which has a higher energy ?

(a) A photon of violet light with wave length  $4000 \text{ \AA}$

(b) A photon of red light with wave length  $7000 \text{ \AA}$

**Soluiton** (a) Violet light :  $E_{\text{violet}} = \frac{hc}{\lambda} = \frac{6.626 \times 10^{-34} \text{ Js} \times 3 \times 10^8 \text{ ms}^{-1}}{4000 \times 10^{-10} \text{ m}} = 4.97 \times 10^{-19} \text{ joule}$

$$\text{(b) Red light : } E_{\text{red}} = \frac{hc}{\lambda} = \frac{6.626 \times 10^{-34} \text{ Js} \times 3 \times 10^8 \text{ ms}^{-1}}{7000 \times 10^{-10} \text{ m}} = 2.8 \times 10^{-19} \text{ joule}$$

So,  $E_{\text{violet}} > E_{\text{red}}$

## 2.6 BOHR'S ATOMIC MODEL

### Some Important formulae :

- This model was based on quantum theory of radiation and classical laws of physics.
- Bohr model is applicable only for single electron species like H,  $\text{He}^+$ ,  $\text{Li}^{2+}$  etc.
- Bohr model is based on particle nature of electron.

$$\text{Coulombic force} = \frac{kq_1q_2}{r^2}$$

$$\text{Centrifugal force} = \frac{mv^2}{r}$$

$$\text{Angular momentum} = mvr$$



## Important postulates :

### 1<sup>st</sup> Postulate :

- Atom has a nucleus where all protons and neutrons are present.
- The size of nucleus is very small and it is present at the centre of the atom.

### 2<sup>nd</sup> Postulate :

- Negatively charged electron revolve around the nucleus in the same way as the planets revolve around the sun.
- The path of electron is circular.
- The attraction force (Coulombic or electrostatic force) between nucleus and electron is equal to the centrifugal force on electron.

i.e. Attraction force towards nucleus = centrifugal force away from nucleus.

### 3<sup>rd</sup> Postulate :

- Electrons can revolve only in those orbits in which angular momentum ( $mvr$ ) of electron is integral multiple

of  $\frac{h}{2\pi}$  i.e.  $\boxed{mvr = \frac{nh}{2\pi}} = n\hbar \quad \hbar = \frac{h}{2\pi}$

where :  $n = +ve$  integer number ( $n = 1, 2, 3, 4, \dots$ ) or ( $n \in \mathbb{I}^+$ )

$h$  = Planck's constant

$\pi$  = Constant

- Angular momentum can have values such as  $\frac{h}{2\pi}, 2\frac{h}{2\pi}, 3\frac{h}{2\pi}, 4\frac{h}{2\pi}, 5\frac{h}{2\pi}, \dots$  but cannot have fractional values such as  $1.5\frac{h}{2\pi}, 1.2\frac{h}{2\pi}, 0.5\frac{h}{2\pi}, \dots$

### 4<sup>th</sup> Postulate :

- The orbits in which electron can revolve are known as **stationary orbits** because in these orbits energy of electron is always constant.

### 5<sup>th</sup> Postulate :

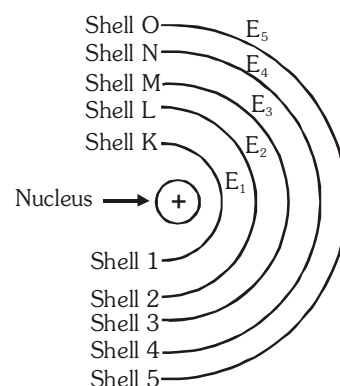
- Each stationary orbit is associated with definite amount of energy therefore these orbits are also called as energy levels and are numbered as 1, 2, 3, 4, 5, .... or K, L, M, N, O, .... from the nucleus outwards.

### 6<sup>th</sup> Postulate

- The emission or absorption of energy in the form of photon can only occur when electron jumps from one stationary state to another & it is

$$\boxed{\Delta E = E_{\text{higher}} - E_{\text{lower}} = E_{n_2} - E_{n_1}} = \text{Energy of a quantum}$$
$$= h\nu = \text{Bohr's frequency condition}$$

- Energy is absorbed when electron jumps from inner to outer orbit and is emitted when electron moves from outer to inner orbit.
- $n_2 > n_1$  whether emission or absorption of energy will occur.



## BEGINNER'S BOX-2

1. Electromagnetic radiation travels through vacuum at a speed of  
 (1) 186000 m/s                      (2) 125 m/s                      (3)  $3.00 \times 10^8$  m/s                      (4) It depends upon wavelength
2. What is the wavelength (Å) of a photon that has an energy of  $4.38 \times 10^{-18}$  J  
 (1) 454 Å                      (2)  $2.3 \times 10^7$  Å                      (3)  $6.89 \times 10^{15}$  Å                      (4)  $1.45 \times 10^{-15}$  Å
3. A 1kw radio transmitter operates at a frequency of 800 Hz. How many photons per second does it emit.  
 (1)  $1.71 \times 10^{21}$                       (2)  $1.88 \times 10^{33}$                       (3)  $6.02 \times 10^{23}$                       (4)  $2.85 \times 10^{20}$
4. Bohr's theory is not applicable to  
 (1) He                      (2)  $\text{Li}^{+2}$                       (3)  $\text{He}^+$                       (4) H atom

### 2.7 APPLICATION OF BOHR'S MODEL

#### (A) Radius of Various Orbits (Shell)

$$\begin{aligned} \text{Coulombic force} &= \frac{Kq_1q_2}{r^2} \\ &= \frac{KZe \cdot e}{r^2} = \frac{KZe^2}{r^2} \end{aligned}$$

Where  $K = 9 \times 10^9 \text{ Nm}^2/\text{coulomb}^2$

As we know – Coulombic force = Centrifugal force

$$\frac{KZe^2}{r^2} = \frac{mv^2}{r} \quad \text{or} \quad v^2 = \frac{KZe^2}{mr} \quad \dots\dots\dots(1)$$

$$\text{As we know – } mvr = \frac{nh}{2\pi} \quad \text{or} \quad v = \frac{nh}{2\pi mr} \quad \dots\dots\dots(2)$$

Putting the value of v from eq<sup>n</sup>. (2) to eq<sup>n</sup>. (1)

$$\left( \frac{nh}{2\pi mr} \right)^2 = \frac{KZe^2}{mr} \quad \text{or} \quad \frac{n^2 h^2}{4\pi^2 m^2 r^2} = \frac{KZe^2}{mr}$$

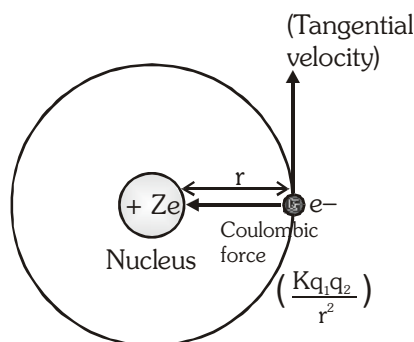
$$\boxed{r = \frac{n^2 h^2}{4\pi^2 m K Z e^2}} \quad \dots\dots\dots(3)$$

Putting the value of  $\pi$ ,  $h$ ,  $m$ ,  $K$ , &  $e$  (Constants) in the above eq<sup>n</sup>. (3)

$$r = 0.529 \times 10^{-8} \times \frac{n^2}{Z} \text{ cm} \quad \{1\text{Å} = 10^{-10}\text{m} = 10^{-8}\text{cm}\}$$

$$\boxed{r_n = 0.529 \times \frac{n^2}{Z} \text{ Å}}$$

This formula is only applicable for hydrogen and hydrogen like species i.e. species containing single electron.



**(B) Velocity of an electron**

Since coulombic force = Centrifugal force

$$\frac{KZe^2}{r^2} = \frac{mv^2}{r} \quad \text{or} \quad v^2 = \frac{KZe^2}{mr} \quad \dots\dots\dots(1)$$

Putting the value of Angular momentum

$$mvr = \frac{nh}{2\pi} \quad \text{or,} \quad KZe^2 = \frac{nh}{2\pi}(v)$$

$$v = \frac{2\pi KZe^2}{nh}$$

Putting the value of  $\pi$ ,  $k$ ,  $e$  &  $h$

$$v = 2.188 \times 10^6 \frac{Z}{n} \text{m/s}$$

**Illustrations**

**Illustration 16.** Calculate the radius of 1<sup>st</sup>, 2<sup>nd</sup>, 3<sup>rd</sup>, 4<sup>th</sup> Bohr's orbit of hydrogen.

**Solution** Radius of Bohr's orbit  $r = 0.529 \times \frac{n^2}{Z} \text{ \AA}$

(a) Radius of I<sup>st</sup> orbit :  $r = 0.529 \times \frac{1^2}{1} \text{ \AA} = 0.529 \text{ \AA}$

(b) Radius of II<sup>nd</sup> orbit :  $r = 0.529 \times \frac{2^2}{1} = 0.529 \times 4 = 2.116 \text{ \AA}$

(c) Radius of III<sup>rd</sup> orbit :  $r = 0.529 \times \frac{3^2}{1} = 0.529 \times 9 = 4.761 \text{ \AA}$

(d) Radius of 4<sup>th</sup> orbit :  $r = 0.529 \times \frac{4^2}{1} = 0.529 \times 16 = 8.464 \text{ \AA}$

**Illustration 17.** Calculate the radius ratio of 3<sup>rd</sup> & 5<sup>th</sup> orbit of He<sup>+</sup>.

**Solution**  $\therefore r = 0.529 \times \frac{n^2}{Z} \text{ \AA}$  and Atomic Number of He = 2

$\therefore r_3 = 0.529 \times \frac{(3)^2}{2} = 0.529 \times \frac{9}{2}$  and  $r_5 = 0.529 \times \frac{(5)^2}{2} = 0.529 \times \frac{25}{2}$

Therefore  $\frac{r_3}{r_5} = \frac{0.529 \times \frac{(3)^2}{2}}{0.529 \times \frac{(5)^2}{2}} = \frac{9}{25}$  or  $r_3 : r_5 = 9 : 25$

**Illustration 18.** Calculate the radius ratio of 2<sup>nd</sup> orbit of hydrogen and 3<sup>rd</sup> orbit of Li<sup>+2</sup>.

**Solution** Atomic number of H = 1, Atomic number of Li = 3,

2<sup>nd</sup> orbit radius of Hydrogen  $(r_2)_H = 0.529 \times \frac{2^2}{1}$

3<sup>rd</sup> orbit radius of Li<sup>+2</sup>  $(r_3)_{Li^{+2}} = 0.529 \times \frac{3^2}{3}$

$\therefore \frac{(r_2)_H}{(r_3)_{Li^{+2}}} = \frac{0.529 \times \frac{2^2}{1}}{0.529 \times \frac{3^2}{3}} = \frac{4}{3} \quad \therefore (r_2)_H : (r_3)_{Li^{+2}} = 4 : 3$



**Illustration 18.** Calculate the radius ratio of 2<sup>nd</sup> excited state of H & 1<sup>st</sup> excited state of Li<sup>+</sup>

**Solution** 2<sup>nd</sup> excited state, means e<sup>-</sup> is present in 3<sup>rd</sup> shell of hydrogen  $r_3 = 0.529 \times \frac{(3)^2}{1} = 0.529 \times 9$

1<sup>st</sup> excited state, means e<sup>-</sup> exist in 2<sup>nd</sup> shell of Li<sup>+</sup>  $r_2 = 0.529 \times \frac{(2)^2}{3} = 0.529 \times \frac{4}{3}$

$$\frac{\text{radius of 2}^{\text{nd}} \text{ excited state of hydrogen}}{\text{radius of 1}^{\text{st}} \text{ excited state of Li}^{+2}} = \frac{(r_3)_H}{(r_2)_{\text{Li}^{+2}}} = \frac{0.529 \times \frac{9}{1}}{0.529 \times \frac{4}{3}} = \frac{27}{4}$$

**Illustration 19.** Calculate velocity of an electron placed in the third orbit of the hydrogen atom. Also calculate the number of revolutions per second that this electron makes around the nucleus.

**Solution** Velocity of electron in 3<sup>rd</sup> orbit :

$$\therefore V_n = 2.182 \times 10^6 \times \frac{Z}{n} \text{ ms}^{-1}$$

$$\therefore V_3 = 2.182 \times 10^6 \times \frac{1}{3} \text{ ms}^{-1} = 7.27 \times 10^5 \text{ ms}^{-1}$$

No. of revolution per second

$$= \frac{v_n}{2\pi r_3} = \frac{v_n}{2\pi \left( \frac{n^2 a_0}{Z} \right)} = \frac{7.27 \times 10^5}{2 \times 3.14 \times 9 \times 0.529 \times 10^{-10}} = 2.43 \times 10^{14} \text{ r.p.s.}$$

**Illustration 20.** How much time an e<sup>-</sup> will take for one complete revolution in 2<sup>nd</sup> orbit of He<sup>+</sup>?

**Solution** time taken =  $\frac{\text{distance}}{\text{velocity}} = \frac{2\pi r}{v} = \frac{2 \times 3.14 \times 0.529 \times \frac{4}{2} \times 10^{-10} \text{ m}}{2.18 \times 10^6 \times \frac{2}{2} \text{ ms}^{-1}} = 3.05 \times 10^{-16} \text{ s}$

### (C) Energy of an electron

Let the total energy of an electron be E. It is the sum of kinetic and potential energy.

$$\text{i.e. } E = \text{K.E.} + \text{P.E.}$$

$$E = \left( \frac{1}{2} mv^2 \right) + \left( \frac{Kq_1 q_2}{r} \right) \quad \left[ \text{P.E.} = -\frac{KZe^2}{r} \right]$$

$$E = \frac{1}{2} mv^2 + \frac{K.Ze.(-e)}{r} = \frac{1}{2} mv^2 - \frac{KZe^2}{r} \quad \left[ \text{KE} = \frac{1}{2} mv^2 = \frac{KZe^2}{2r} \right]$$

$$E = \frac{KZe^2}{2r} - \frac{KZe^2}{r} = -\frac{KZe^2}{2r}$$

Putting the value of r from eq. (3)

$$E_n = -\frac{KZe^2 \times 4\pi^2 m KZe^2}{2n^2 h^2} \quad \text{or} \quad E_n = -\frac{2\pi^2 m K^2 Z^2 e^4}{n^2 h^2}$$

Putting the value of  $\pi$ , K, e, m, h, we get :

$$E_n = -2.18 \times 10^{-18} \times \frac{Z^2}{n^2} \text{ J/atom} \quad \text{or} \quad E_n = -13.6 \times \frac{Z^2}{n^2} \text{ eV/atom}$$

This formula is applicable for hydrogen atom & hydrogen like species i.e. single electron species.

Since n can have only integral values, it follows that total energy of the e<sup>-</sup> is quantised.

The -ve sign indicates that the electron is bonded towards nucleus.



### Some extra points :

- (i)  $K.E = \frac{KZe^2}{2r}$  i.e.  $K.E. \propto \frac{1}{r}$  On increasing radius, K.E. decreases.
- (ii)  $P.E. = -\frac{KZe^2}{r}$  i.e.  $P.E. \propto -\frac{1}{r}$  On increasing radius, P.E. increases.
- (iii)  $E = -\frac{KZe^2}{2r}$  i.e.  $E \propto -\frac{1}{r}$  On increasing radius, total energy increases.

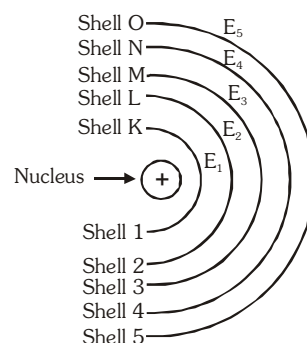
**Conclusion :**  $P.E = (-)2KE$   $KE = (-)E$   $P.E = 2E$

Energy difference between two energy levels :

$$E_{n_2} - E_{n_1} = -13.6 \times Z^2 \left[ \frac{1}{n_2^2} - \frac{1}{n_1^2} \right]$$

Energy level for H atom can be represented as follows :

$n = 6$ or P	$E_6 = -0.38 \text{ eV}$	
$n = 5$ or O	$E_5 = -0.54 \text{ eV}$	
$n = 4$ or N	$E_4 = -0.85 \text{ eV}$	$E_5 - E_4 = 0.31 \text{ eV}$
$n = 3$ or M	$E_3 = -1.51 \text{ eV}$	$E_4 - E_3 = 0.66 \text{ eV}$
$n = 2$ or L	$E_2 = -3.4 \text{ eV}$	$E_3 - E_2 = 1.89 \text{ eV}$
$n = 1$ or K	$E_1 = -13.6 \text{ eV}$	$E_2 - E_1 = 10.2 \text{ eV}$
i.e. $(E_2 - E_1) > (E_3 - E_2) > (E_4 - E_3) > (E_5 - E_4) \dots$		



### Important Definitions :-

- (i) **Ionization energy :** Minimum amount of energy required to liberate an electron from the ground state of an isolated atom is called as ionization energy.  
 $n_1 = 1; n_2 = \infty$
- (ii) **Separation energy :** Minimum energy required to remove an electron from its excited state is called as separation energy.  
 $n_1 = 2, 3, 4, 5, \dots; n_2 = \infty$
- (iii) **Excitation energy :** Amount of energy required to shift an electron from ground state to any excited state is called as excitation energy.  
 $n_1 = 1; n_2 = 2, 3, 4, 5, \dots$

Note : All these kinds of energy are always positive.

## Illustrations

**Illustration 21.** If the total energy of an electron is  $-1.51 \text{ eV}$  in hydrogen atom then find out K.E, P.E, orbit, radius and velocity of the electron in that orbit.

**Solution**

- (i)  $K.E = -E = 1.51 \text{ eV}$
- (ii)  $PE = 2 \times E = -2 \times 1.51 = -3.02 \text{ eV}$
- (iii)  $\therefore E = -13.6 \times \frac{Z^2}{n^2} \text{ eV}$  or  $-1.51 = -13.6 \times \frac{1^2}{n^2}$   
 $\Rightarrow n^2 = \frac{-13.6}{-1.51} = 9 \quad \therefore n = 3 \quad \text{i.e. } 3^{\text{rd}} \text{ orbit}$
- (iv)  $r = 0.529 \times \frac{n^2}{Z} = 0.529 \times \frac{3 \times 3}{1} = 0.529 \times 9 = 4.761 \text{ \AA}$
- (v)  $v = 2.188 \times 10^8 \times \frac{Z}{n} = 2.188 \times 10^8 \times \frac{1}{3} \text{ cm/s} = 0.729 \times 10^8 \text{ cm/s}$



**Illustration 22.** Calculate the energy of  $\text{Li}^{+2}$  ion for 2<sup>nd</sup> excited state

**Solution**  $E = -13.6 \times \frac{Z^2}{n^2}$   $\therefore Z = 3$  and electron exist in 2<sup>nd</sup> excited state, means electron present in 3<sup>rd</sup> shell  
i.e.  $n = 3$

$$\therefore E = -13.6 \times \frac{(3)^2}{(3)^2} = -13.6 \text{ eV/atom}$$

**Illustration 23.** Calculate the ratio of energies of  $\text{He}^+$  for 1<sup>st</sup> & 2<sup>nd</sup> excited state .

**Solution**  $\frac{\text{Energy of } (\text{He}^+) \text{ 1}^{\text{st}} \text{ Excited state}}{\text{Energy of } (\text{He}^+) \text{ 2}^{\text{nd}} \text{ Excited state}} = \frac{\text{Energy of } (\text{He}^+) \text{ 2}^{\text{nd}} \text{ shell}}{\text{Energy of } (\text{He}^+) \text{ 3}^{\text{rd}} \text{ shell}} = \frac{-13.6 \times \frac{(2)^2}{(2)^2}}{-13.6 \times \frac{(2)^2}{(3)^2}} = \frac{9}{4}$

**Illustration 24.** The ionization energy for the hydrogen atom is 13.6 eV then the required energy in eV to excite it from the ground state to 1<sup>st</sup> excited state

**Solution** Ionization energy = 13.6 eV i.e. Energy in ground state = -13.6 eV  
Energy of 1<sup>st</sup> excited state i.e. 2<sup>nd</sup> orbit = -3.4 eV  
so,  $E_2 - E_1 = -3.4 + 13.6 = 10.2 \text{ eV}$

### GOLDEN KEY POINTS

- Bohr's atomic model is applicable only for monoelectronic species like H,  $\text{He}^+$ ,  $\text{Li}^{+2}$ ,  $\text{Na}^{10+}$ ,  $\text{U}^{91+}$  etc.

$$E_{z,n} = E_H \times \frac{Z^2}{n^2}$$

if z is same

 $E_n = E_H \times \frac{1}{n^2}$

if n is same

 $E_z = E_H \times Z^2$

### BEGINNER'S BOX-3

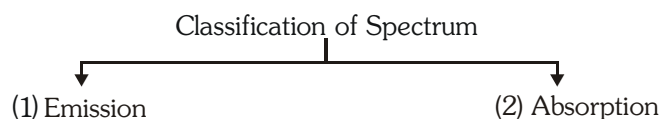
- In which of the following is the radius of the first orbit minimum ?  
(1) A Hydrogen atom (2) A tritium atom  
(3) Triply ionized beryllium (4) Double ionized helium
- The energy needed to excite a hydrogen atom from its ground to its third excited state is  
(1) 12.1 ev (2) 10.2 ev (3) 0.85 ev (4) 12.75 ev
- The ionisation energy of a hydrogen atom is 13.6 ev. The energy of the ground level in doubly ionised lithium is  
(1) - 28.7 ev (2) - 54.4 ev (3) -122.4 ev (4) - 13.6 ev
- What would be the radius of 2<sup>nd</sup> excited state in  $\text{Li}^{+2}$  ion ?  
(1) 0.529  $\text{\AA}^\circ$  (2) 1.51  $\text{\AA}^\circ$  (3) 0.2645  $\text{\AA}^\circ$  (4) 0.5299  $\text{\AA}^\circ$
- 2<sup>nd</sup> separation energy of an electron in H atom  
(1) 27.2 ev (2) 1.57 ev (3) 3.4 ev (4) 13.6 ev
- How much energy would be required by an electron while moving from ground state to 3<sup>rd</sup> excited state of  $\text{He}^+$  ion.  
(1) 40.8 ev (2) 10.2 ev (3) 51 ev (4) 48.35 ev





## 2.8 SPECTRUM

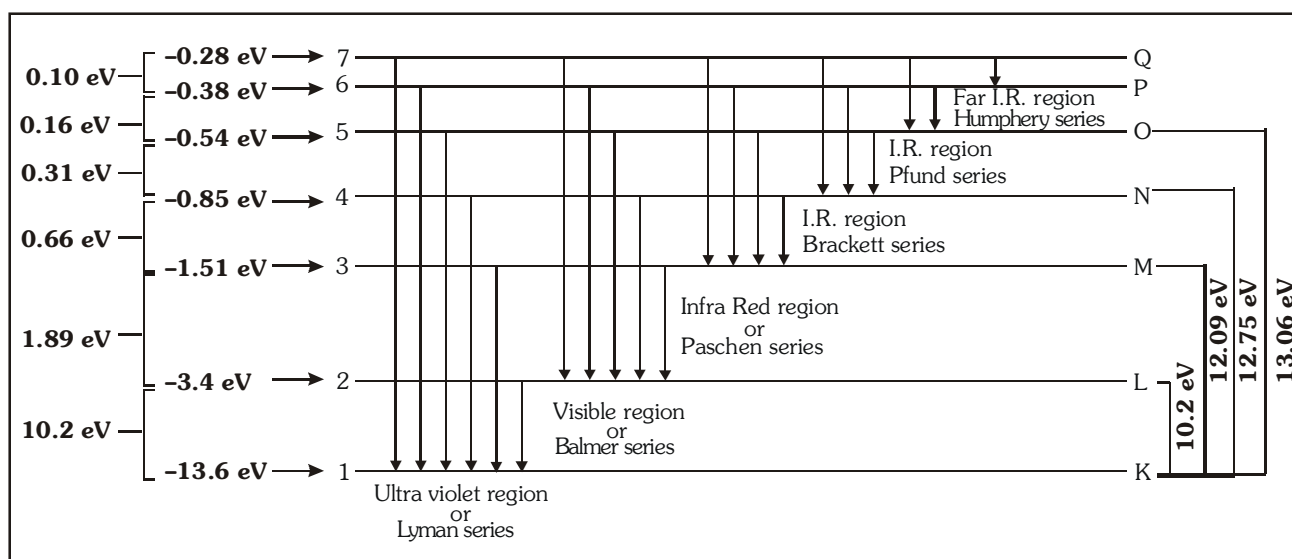
When a radiation is passed through a spectroscope (prism) for the dispersion of the radiation, the pattern (photograph) obtained on the screen (photographic plate) is called as spectrum of the given radiation



### HYDROGEN SPECTRUM

When an electric excitation is applied on hydrogen atomic gas at low pressure, a bluish light is emitted. When a ray of this light is passed through a prism, a spectrum of several isolated sharp lines is obtained. The wavelength of various lines show that spectrum lines lie in Visible, Ultraviolet and Infra red region. These lines are grouped into different series.

Series	Discovered by	regions	$n_2 \rightarrow n_1$	No. of lines
Lyman	Lyman	U.V. region	$n_2 = 2, 3, 4 \dots / n_1 = 1$	$n_2 - 1$
Balmer	Balmer	Visible region	$n_2 = 3, 4, 5 \dots / n_1 = 2$	$n_2 - 2$
Paschen	Paschen	Infra red (I.R.)	$n_2 = 4, 5, 6 \dots / n_1 = 3$	$n_2 - 3$
Brackett	Brackett	I.R. region	$n_2 = 5, 6, 7 \dots / n_1 = 4$	$n_2 - 4$
Pfund	Pfund	I.R. region	$n_2 = 6, 7, 8 \dots / n_1 = 5$	$n_2 - 5$
Humphery	Humphery	Far I.R. region	$n_2 = 7, 8, 9 \dots / n_1 = 6$	$n_2 - 6$



#### Similar words

- First line / Starting line / Initial line ( $\lambda_{\max}$  and  $\nu_{\min}$ )
- Last line / limiting line / marginal line ( $\lambda_{\min}$  and  $\nu_{\max}$ )
- First line of any series =  $\alpha$  line

Second line of any series =  $\beta$  line

Third line of any series =  $\gamma$  line



### Calculation of number of spectral lines

$$(a) \text{ Total number of spectral lines} = 1 + 2 + \dots (n_2 - n_1) = \frac{(n_2 - n_1)(n_2 - n_1 + 1)}{2}$$

Where :  $n_2$  = higher energy level;  $n_1$  = lower energy level

If  $n_1 = 1$  (ground state)

$$\text{Total number of spectral lines} = \frac{(n_2 - 1)n_2}{2} = \frac{n(n-1)}{2}$$

$$(b) \text{ Number of spectral lines which falls in a particular series} = (n_2 - n_1)$$

where  $n_2$  = higher energy level,  $n_1$  = Fixed lower energy level of each series.

### RYDBERG FORMULA

In 1890, Rydberg gave a very simple theoretical equation for the calculation of the wavelength of various lines of hydrogen like spectrum

$$\bar{\nu} = \frac{1}{\lambda} = RZ^2 \left[ \frac{1}{n_1^2} - \frac{1}{n_2^2} \right]$$

where  $R$  = Rydberg constant =  $109678 \text{ cm}^{-1} = 109700 \text{ cm}^{-1} = 10970000 \text{ m}^{-1} = 1.1 \times 10^7 \text{ m}^{-1}$

$$\frac{1}{R} = 9.12 \times 10^{-6} \text{ cm} = 912 \text{ \AA}$$

### Derivation of Rydberg formula :

$$\Delta E = E_{n_2} - E_{n_1}$$

$$\Delta E = \frac{-2\pi^2 m K^2 Z^2 e^4}{n_2^2 h^2} - \left[ \frac{-2\pi^2 m K^2 Z^2 e^4}{n_1^2 h^2} \right]$$

$$= \frac{2\pi^2 m K^2 Z^2 e^4}{n_1^2 h^2} - \frac{2\pi^2 m K^2 Z^2 e^4}{n_2^2 h^2} \quad \left( \because \Delta E = h\nu = \frac{hc}{\lambda} \right)$$

$$\frac{hc}{\lambda} = \frac{2\pi^2 m K^2 Z^2 e^4}{h^2} \left[ \frac{1}{n_1^2} - \frac{1}{n_2^2} \right] \quad \text{or} \quad \frac{1}{\lambda} = \frac{2\pi^2 m K^2 e^4 Z^2}{ch^3} \left[ \frac{1}{n_1^2} - \frac{1}{n_2^2} \right]$$

where  $\frac{2\pi^2 m K^2 e^4}{ch^3}$  is a constant which is equal to Rydberg constant ( $R$ ).

$$\frac{1}{\lambda} = RZ^2 \left[ \frac{1}{n_1^2} - \frac{1}{n_2^2} \right]$$

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## Illustrations

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**Illustration 25.** Calculate the wavelength of 1<sup>st</sup> line of Balmer series in Hydrogen spectrum.

**Solution** For first line of Balmer series  $n_1 = 2, n_2 = 3$

$$\frac{1}{\lambda} = R(1)^2 \left[ \frac{1}{4} - \frac{1}{9} \right] = R \left[ \frac{9-4}{36} \right] = R \left[ \frac{5}{36} \right]$$

$$\Rightarrow \lambda = \frac{36}{5R} = \frac{36}{5} \times \frac{1}{R} = \frac{36}{5} \times 9.12 \times 10^{-6} \text{ cm} = 65.66 \times 10^{-6} \text{ cm} = 6566 \text{ \AA}$$



**Illustration 26.** Calculate the frequency of the last line of the Lyman series in hydrogen spectrum.

**Solution** For last line of Lyman series  $n_1 = 1$ ,  $n_2 = \infty$

$$\frac{1}{\lambda} = RZ^2 \left( \frac{1}{n_1^2} - \frac{1}{n_2^2} \right) = R \left( \frac{1}{1} - 0 \right) = R$$

$$\Rightarrow \nu = \frac{c}{\lambda} = c \times \frac{1}{\lambda} = c \times R = 3 \times 10^{10} \text{ cm s}^{-1} \times 109678 \text{ cm}^{-1} = 3.29 \times 10^{15} \text{ s}^{-1}$$

**Illustration 27.** Calculate the wavelength of 3<sup>rd</sup> line of Brackett series in hydrogen spectrum.

**Solution** For 3<sup>rd</sup> line of Brackett series  $n_1 = 4$ ,  $n_2 = 7$

$$\frac{1}{\lambda} = RZ^2 \left[ \frac{1}{(4)^2} - \frac{1}{(7)^2} \right] = R \left[ \frac{1}{16} - \frac{1}{49} \right] = R \left[ \frac{49-16}{16 \times 49} \right] = R \frac{33}{784}$$

$$\text{Therefore, } \lambda = \frac{784}{33R} = \frac{784}{33} \times 912 \text{ \AA} = 21667 \text{ \AA}$$

**Illustration 28.** The wave number of 1<sup>st</sup> line of Balmer series of hydrogen spectrum is  $15200 \text{ cm}^{-1}$  The wave number of 1<sup>st</sup> line of Balmer series of  $\text{Li}^{+2}$  spectrum will be ?

**Solution** Wave number of 1<sup>st</sup> line of Balmer series of hydrogen spectrum.  $\bar{\nu} = \frac{1}{\lambda} = RZ^2 \left( \frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$

$$(\text{for H, } Z = 1) \quad \bar{\nu} = R \left( \frac{1}{n_1^2} - \frac{1}{n_2^2} \right) = 15200 \text{ cm}^{-1}$$

Wave number of 1<sup>st</sup> line of Balmer series of  $\text{Li}^{+2}$  ion is.

$$\bar{\nu} = Z^2 \times R \left( \frac{1}{n_1^2} - \frac{1}{n_2^2} \right) \quad \{ \because Z = 3 \text{ for } \text{Li}^{+2} \}$$

$$\therefore \bar{\nu} = 3^2 \times 15200 = 9 \times 15200 = 136800 \text{ cm}^{-1}$$

**Illustration 29.** Calculate the ratio of maximum  $\lambda$  of Lyman & Balmer series ?

**Solution**  $E \propto \nu \propto \frac{1}{\lambda}$

$$\frac{\text{Maximum } \lambda \text{ of Lyman series}}{\text{Maximum } \lambda \text{ of Balmer series}} = \frac{1^{\text{st}} \text{ line of Lyman series}}{1^{\text{st}} \text{ line of Balmer series}}$$

$$\frac{\lambda_{\text{Lyman}}}{\lambda_{\text{Balmer}}} = \frac{\frac{1}{\lambda_B}}{\frac{1}{\lambda_L}} = \frac{R \left[ \frac{1}{2^2} - \frac{1}{3^2} \right]}{R \left[ \frac{1}{1^2} - \frac{1}{2^2} \right]} = \frac{\frac{1}{4} - \frac{1}{9}}{\frac{1}{1} - \frac{1}{4}} = \frac{\frac{5}{36}}{\frac{3}{4}} = \frac{5}{36} \times \frac{4}{3} = \frac{5}{27}$$



**Illustration 30.** In a hydrogen spectrum if electron moves from 7 to 1 orbit by transition in multi steps then find out the total number of lines in the spectrum.

**Solution**

Lyman	=	$(n_2 - 1) = 7 - 1 = 6$
Balmer	=	$(n_2 - 2) = 7 - 2 = 5$
Paschen	=	$(n_2 - 3) = 7 - 3 = 4$
Bracket	=	$(n_2 - 4) = 7 - 4 = 3$
Pfund	=	$(n_2 - 5) = 7 - 5 = 2$
Humphrey	=	$(n_2 - 6) = 7 - 6 = 1$
Total	=	21

Total number of lines can be calculated as follows :

$$\text{Total number of lines} = \frac{(n_2 - n_1)[(n_2 - n_1) + 1]}{2} = \frac{(7 - 1)(6 + 1)}{2} = \frac{42}{2} = 21$$

**Illustration 31.** In a hydrogen spectrum if electron moves from 6<sup>th</sup> to 2<sup>nd</sup> orbit by transition in multi steps then find out the number of lines in spectrum

**Solution** Total number of line = 4 + 3 + 2 + 1 = 10

$$\text{or Total number of lines} = \frac{(n_2 - n_1)[(n_2 - n_1) + 1]}{2} = \frac{(6 - 2)(4 + 1)}{2} = \frac{4 \times 5}{2} = 10$$

**Illustration 32.** A certain electronic transition from an excited state to Ground state of the Hydrogen atom in one or more steps gives rise to 5 lines in the ultra violet region of the spectrum. How many lines does this transition produce in the Infra red region of the spectrum?

**Solution** **(Lyman Series) ultra violet region :** 5 Lines i.e.  $e^-$  is coming from 6<sup>th</sup> to 1<sup>st</sup> Orbit

$$n_2 - 1 = 5 \quad \text{or} \quad n_2 = 6$$

Infrared region line

$$(i) \text{ Paschen series} = (6 - 3) = 3 \quad (ii) \text{ Bracket} = (6 - 4) = 2 \quad (iii) \text{ Pfund} = (6 - 5) = 1$$

**Total Number of lines are = 6**

**Illustration 33.** In H atom if the electron moves from  $n^{\text{th}}$  orbit to 1<sup>st</sup> orbit by transition in multi steps, then the total number of lines observed in the spectrum are 10, then find out the value of n.

**Solution** Total number of lines =  $\frac{(n_2 - n_1)[(n_2 - n_1) + 1]}{2}$

$$\text{So,} \quad 10 = \frac{(n - 1)(n - 1 + 1)}{2}$$

$$\text{or} \quad 20 = (n - 1)(n)$$

$$n^2 - n - 20 = 0$$

$$n^2 - 5n + 4n - 20 = 0$$

$$n(n - 5) + 4(n - 5) = 0$$

$$(n + 4)(n - 5) = 0 \quad \Rightarrow \quad n = 5$$

### Limitation of the Bohr's model :

- (1) Bohr's theory does not explain the spectrum of multi electron atom.
- (2) Why the Angular momentum of the revolving electron is equal to  $\frac{nh}{2\pi}$ , has not been explained by Bohr's theory.
- (3) Bohr inter related quantum theory of radiation and classical laws of physics without any theoretical explanation.
- (4) Bohr's theory does not explain the fine structure of the spectral lines. Fine structure of the spectral line is obtained when spectrum is viewed by spectroscopy of more resolution power.
- (5) Bohr theory does not explain the splitting of spectral lines in the presence of magnetic field (Zeeman's effect) or electric field (Stark's effect)



## BEGINNER'S BOX-4

1. The line spectra of two elements are not identical because
  - (1) The elements don't have the same number of neutrons.
  - (2) They have different mass numbers
  - (3) Their outermost electrons are at different energy levels.
  - (4) They have different valencies.
  
2. In which of the following transition will the wavelength be minimum.
  - (1)  $n = 6$  to  $n = 4$
  - (2)  $n = 4$  to  $n = 2$
  - (3)  $n = 3$  to  $n = 1$
  - (4)  $n = 2$  to  $n = 1$
  
3. The wavelength of third line of the Balmer series for a H atom is
  - (1)  $\frac{21}{100R}$
  - (2)  $\frac{100}{21R}$
  - (3)  $\frac{21R}{100}$
  - (4)  $\frac{100R}{21}$
  
4. When the electron of a hydrogen atom jumps from  $n = 4$  to  $n = 1$  state, the number of spectral lines emitted is
  - (1) 15
  - (2) 6
  - (3) 3
  - (4) 4

### 2.9 WAVE MECHANICAL MODEL OF AN ATOM

This model consists of following

- (A) de-Broglie concept (Dual nature of Matter)
- (B) Heisenberg's Uncertainty principle.

#### (A) THE DUAL NATURE OF MATTER (THE WAVE NATURE OF ELECTRON)

In 1924, a French physicist, **Louis de-Broglie** suggested that if the nature of light is both that of a particle and of a wave, then this dual behavior should be true also for the matter.

- (1) The wave nature of light rays and X-rays is proved on the basis of their interference and diffraction and many facts related to radiations can only be explained when the beam of light rays is regarded as composed of energy corpuscles or photons whose velocity is  $3 \times 10^{10}$  cm/s.
- (2) According to de-Broglie, the wavelength  $\lambda$  of an electron is inversely proportional to its momentum  $p$ .

$$\lambda \propto \frac{1}{p} \quad \text{or} \quad \lambda = \frac{h}{p} \quad (\text{Here } h = \text{Planck's constant, } p = \text{momentum of electron})$$

$$\therefore \text{Momentum } (p) = \text{Mass } (m) \times \text{Velocity } (v) \quad \therefore \lambda = \frac{h}{mv}$$

- (3) The above relation can be proved as follows by using Einstein's equation, Planck's quantum theory and wave theory of light.

Einstein's equation,  $E = mc^2$  where  $E$  is energy,  $m$  is mass of a body and  $c$  is its velocity.

$$\therefore E = hv = h \times \frac{c}{\lambda} \quad (\text{According to Planck's quantum theory}) \quad \dots(i)$$

$$\text{and } c = v\lambda \quad (\text{According to wave theory of light}) \quad \therefore v = \frac{c}{\lambda}$$

But according to Einstein's equation  $E = mc^2 \dots(ii)$

$$\text{From equation (i) \& (ii) : } mc^2 = h \times \frac{c}{\lambda} \quad \text{or} \quad mc = \frac{h}{\lambda} \quad \text{or} \quad p = \frac{h}{\lambda} \quad \text{or} \quad \boxed{\lambda = \frac{h}{p}}$$

- (4) It is clear from the above equation that the value of  $\lambda$  decreases on increasing either  $m$  or  $v$  or both. The wavelength of many fast-moving objects like an aeroplane or a cricket ball, is very low because of their high mass.



### Bohr's theory and de-broglie concept :

- (1) According to de-Broglie, the nature of an electron moving around the nucleus is like a wave that flows in circular orbits around the nucleus.
- (2) If an electron is regarded as a wave, the quantum condition as given by Bohr in his theory is readily fulfilled.
- (3) If the radius of a circular orbit is  $r$ , then its circumference will be  $2\pi r$ .
- (4) We know that according to Bohr theory,  $mvr = \frac{nh}{2\pi}$

$$\text{or } 2\pi r = \frac{nh}{mv} \quad (\because mv = p \text{ momentum})$$

$$\text{or } 2\pi r = \frac{nh}{p} \quad \left( \because \frac{h}{p} = \lambda \text{ de-Broglie equation} \right)$$

$$\therefore 2\pi r = n\lambda \quad (\text{where } n = \text{total number of waves } 1, 2, 3, 4, 5, \dots, \infty \text{ and } \lambda = \text{Wavelength})$$

$$(5) \quad \therefore 2\pi r = \frac{nh}{mv} \quad \text{or} \quad mvr = \frac{nh}{2\pi} \quad \therefore mvr = \text{Angular momentum}$$

Thus  $mvr = \text{Angular momentum}$ , which is a integral multiple of  $\frac{h}{2\pi}$ .

- (6) It is clear from the above description that according to de-Broglie there is similarity between wave theory and Bohr theory.

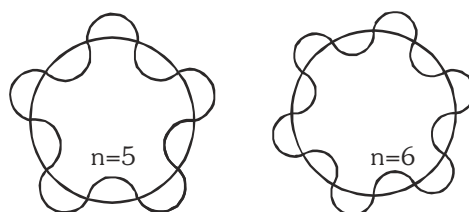


figure : Similarity between de-Broglie waves and Bohr's orbit

### (B) HEISENBERG UNCERTAINTY PRINCIPLE

Bohr's theory considers an electron as a material particle. Its position and momentum can be determined with accuracy. But, when an electron is considered in the form of wave as suggested by de-Broglie, it is not possible to ascertain simultaneously the exact position and velocity of the electron more precisely at a given instant since the wave extends throughout a region of space.

In 1927, Werner Heisenberg presented a principle known as Heisenberg uncertainty principle which states that : "It is impossible to measure simultaneously the exact position and exact momentum of a body as small as an electron."

The uncertainty in measurement of position,  $(\Delta x)$ , and the uncertainty in momentum  $(\Delta p)$  are related by Heisenberg's relationship as

$$\Delta E \times \Delta t \geq \frac{h}{4\pi} \quad \text{or} \quad \Delta E \times \Delta t \geq \frac{h}{4\pi}$$

where  $h$  is Planck's constant.

- (i) When  $\Delta x = 0$ ,  $\Delta v = \infty$
- (ii) When  $\Delta v = 0$ ,  $\Delta x = \infty$  So, if the position is known quite accurately, i.e.,  $\Delta x$  is very small,  $\Delta v$  becomes large and vice-versa.



## GOLDEN KEY POINTS

- **de-Broglie wavelength in terms of kinetic energy.**

$$\text{Kinetic Energy (K.E.)} = \frac{1}{2}mv^2 \text{ or } m \times \text{K.E.} = \frac{1}{2}m^2v^2 \text{ or } m^2v^2 = 2m \text{ K.E. or } mv = \sqrt{2m \text{ K.E.}}$$

$$\text{But } \lambda = \frac{h}{mv} \quad \therefore \quad \lambda = \frac{h}{\sqrt{2m \text{ K.E.}}} \quad \left( \because mv = \sqrt{2m \text{ K.E.}} \right)$$

- **When a charged particle carrying Q coulomb charge is accelerated by applying potential difference of V volts, then :-**

$$\text{K.E.} = Q \times V \text{ Joule}$$

$$\text{But } \lambda = \frac{h}{\sqrt{2m \text{ K.E.}}} \quad \therefore \quad \lambda = \frac{h}{\sqrt{2mQV}} \quad \left[ \text{For electron } \left( \lambda = \sqrt{\frac{150}{V}} \text{ \AA} \right) \right] = \frac{12.25}{\sqrt{V}} \text{ \AA}$$

- The wave nature of electron was verified experimentally by Davisson and Germer.
- de-Broglie hypothesis is applicable to macroscopic as well as microscopic objects but it has no physical significance for macroscopic objects.

- Remember  $\frac{h}{4\pi} = 0.527 \times 10^{-34} \text{ J sec}$

## Illustrations

**Illustration 34.** The mass of a particle is 1 mg and its velocity is  $4.5 \times 10^5 \text{ cm per second}$ . What should be the wavelength of this particle if  $h = 6.652 \times 10^{-27} \text{ erg second}$ .

(1)  $1.4722 \times 10^{-24} \text{ cm}$  (2)  $1.4722 \times 10^{-29} \text{ cm}$  (3)  $1.4722 \times 10^{-32} \text{ cm}$  (4)  $1.4722 \times 10^{-34} \text{ cm}$

**Solution** Given that  $m = 1 \text{ mg} = 1 \times 10^{-3} \text{ g}$ ,  $v = 4.5 \times 10^5 \text{ cm s}^{-1}$ ,  $h = 6.652 \times 10^{-27} \text{ erg s}$ .

$$\therefore \lambda = \frac{h}{mv} = \frac{6.625 \times 10^{-27} \text{ erg s}}{1 \times 10^{-3} \text{ g} \times 4.5 \times 10^5 \text{ cm s}^{-1}} = 1.4722 \times 10^{-29} \text{ cm}$$

**Illustration 35.** Which of the following should be the wavelength of an electron if its mass is  $9.1 \times 10^{-31} \text{ kg}$  and its velocity is  $1/10$  of that of light and the value of  $h$  is  $6.6252 \times 10^{-34} \text{ joule second}$ ?

(1)  $2.446 \times 10^{-7} \text{ metre}$  (2)  $2.246 \times 10^{-9} \text{ metre}$  (3)  $2.246 \times 10^{-11} \text{ metre}$  (4)  $2.246 \times 10^{-13} \text{ metre}$

**Solution** Given that  $m = 9.1 \times 10^{-31} \text{ kg}$ ,  $v = \frac{1}{10}$  of velocity of light

$$\text{or } v = \frac{1}{10} \times 3 \times 10^8 \text{ metre second}^{-1} \text{ i.e. } 3 \times 10^7 \text{ metre second}^{-1}$$

$$h = 6.6252 \times 10^{-34} \text{ joule second}$$

$$\lambda = \frac{h}{mc} = \frac{6.6252 \times 10^{-34} \text{ J.s}}{9.1 \times 10^{-31} \text{ kg} \times 3 \times 10^7 \text{ ms}^{-1}} = \frac{6.6252 \times 10^{-34}}{27.3 \times 10^{-24}}$$

$$= 0.2426 \times 10^{-10} \text{ metre} = 2.426 \times 10^{-11} \text{ metre}$$

**Illustration 36.** A ball weighing 25 g moves with a velocity of  $6.6 \times 10^4 \text{ cm s}^{-1}$  then find out the de-Broglie  $\lambda$  associated with it.

**Solution**  $\lambda = \frac{h}{mv} = \frac{6.6 \times 10^{-34} \times 10^7 \text{ ergs}}{25 \times 6.6 \times 10^4 \text{ cm s}^{-1}} = 0.04 \times 10^{-31} \text{ cm} = 4 \times 10^{-33} \text{ cm}$



**Illustration 37.** If the uncertainty in position of a moving particle is 0 then find out  $\Delta p$  –

**Solution**  $\Delta x \Delta p \geq \frac{h}{4\pi}$  or  $\Delta p \geq \frac{h}{4\pi \Delta x}$  or  $\Delta p \geq \frac{h}{4\pi \times 0}$  or  $\Delta p \geq \infty$

**Illustration 38.** Calculate the uncertainty in the position of a particle when the uncertainty in momentum is (a)  $1 \times 10^{-3} \text{ g cm s}^{-1}$  (b) zero.

**Solution** (a) Given  $\Delta p = 1 \times 10^{-3} \text{ g cm s}^{-1}$ ,  $h = 6.62 \times 10^{-27} \text{ erg s}$ ,  $\pi = 3.142$

According to uncertainty principle

$$\Delta x \Delta p \geq \frac{h}{4\pi} \quad \text{or} \quad \Delta x \geq \frac{h}{4\pi \Delta p} \geq \frac{6.62 \times 10^{-27}}{4 \times 3.142} \times \frac{1}{10^{-3}} \geq 0.527 \times 10^{-24} \text{ cm}$$

(b) When the value of  $\Delta p = 0$ , the value of  $\Delta x$  will be infinity.

**Illustration 39.** The uncertainty in position and velocity of a particle are  $10^{-10} \text{ m}$  and  $5.27 \times 10^{-24} \text{ ms}^{-1}$  respectively. Calculate the mass of the particle ( $h = 6.625 \times 10^{-34} \text{ joule second}$ )

**Solution** According to Heisenberg's uncertainty principle,

$$\Delta x \cdot m \Delta v = \frac{h}{4\pi} \quad \text{or} \quad m = \frac{h}{4\pi \Delta x \Delta v} = \frac{6.625 \times 10^{-34}}{4 \times 3.143 \times 10^{-10} \times 5.27 \times 10^{-24}} = 0.099 \text{ kg}$$

**Illustration 40.** Calculate the uncertainty in velocity of a cricket ball of mass 150 g if the uncertainty in its position is of the order of  $1 \text{ \AA}$  ( $h = 6.6 \times 10^{-34} \text{ kg m}^2 \text{ s}^{-1}$ ).

**Solution**  $\Delta x \cdot m \Delta v = \frac{h}{4\pi} \quad \text{or} \quad \Delta v = \frac{h}{4\pi \Delta x \cdot m} = \frac{6.6 \times 10^{-34}}{4 \times 3.143 \times 10^{-10} \times 0.150}$   
 $= 3.499 \times 10^{-24} \text{ ms}^{-1}$

## 2.10 QUANTUM NUMBERS

To obtain complete information about an electron in an atom 4 identification numbers are required and these identification numbers are called as quantum numbers.

- Principal quantum number ( $n$ )  $\rightarrow$  Shell (Orbit)
- Azimuthal quantum number ( $\ell$ )  $\rightarrow$  Sub shell
- Magnetic quantum number ( $m$ )  $\rightarrow$  Orbital
- Spin quantum number ( $s$ )  $\rightarrow$  Spin of electron

### (a) Principal Quantum Number ( $n$ )

Given By  $\rightarrow$  Bohr

- It represents the name and energy of the shell to which electron belongs and size of orbital.
- The value of  $n$  lies between 1 to  $\infty$   
i.e  $n = 1, 2, 3, 4, \dots, \infty$  corresponding name of shells are K, L, M, N, O,  $\dots$
- Greater the value of  $n$ , greater is the distance from the nucleus.

$$r = 0.529 \times \frac{n^2}{Z} \text{ \AA}$$

$$r_1 < r_2 < r_3 < r_4 < r_5 \dots$$





- Greater the value of  $n$ , greater is the energy of shell  

$$E = -13.6 \times \frac{Z^2}{n^2} \text{ eV/atom}$$

$$E_1 < E_2 < E_3 < E_4 \text{ -----}$$
- Velocity of electron  $v = 2.18 \times 10^6 \frac{Z}{n} \text{ m/s}$   

$$v_1 > v_2 > v_3 \text{ .....}$$
- The angular momentum of a revolving electron is  $mvr = \frac{nh}{2\pi}$   
 Where  $n$  = Principal quantum number.
- The number of electrons in a particular shell is equal to  $2n^2$

**(b) Azimuthal quantum number / Angular quantum number / Secondary quantum number / Subsidiary quantum number ( $\ell$ )**

Given by – Sommerfeld

- It represents the name of the subshell, shape of orbital and orbital angular momentum
- Possible values of ' $\ell$ ' are :-  
 i.e.  $\ell = 0, 1, 2 \text{ ----- } (n-1)$   
 $\ell = 0$  (s Subshell)  
 $\ell = 1$  (p Subshell)  
 $\ell = 2$  (d Subshell)  
 $\ell = 3$  (f Subshell)
- Value of  $\ell$  lies between 0 to  $(n-1)$  in a particular  $n^{\text{th}}$  shell :-  
**Ex.** If  $n = 1$  then  $\ell = 0 \Rightarrow 1s$  i.e. in  $n = 1$  shell, only one subshell 's' is present.  
 If  $n = 2$  then  $\ell = 0, 1 \Rightarrow 2s, 2p$  i.e. in  $n = 2$  shell, two subshell 's' & 'p' are present.  
 If  $n = 3$  then  $\ell = 0, 1, 2 \Rightarrow 3s, 3p, 3d$  i.e. in  $n = 3$  shell, three subshell 's', 'p' & 'd' are present.  
 If  $n = 4$  then  $\ell = 0, 1, 2, 3 \Rightarrow 4s, 4p, 4d, 4f$  i.e. in  $n = 4$  shell, four subshell 's', 'p', 'd' & 'f' are present.
- If the value of  $n$  is same then the order of energy of the various subshell will be  $s < p < d < f$  [valid only for multi-electron species]  
**Ex.**  $4s < 4p < 4d < 4f$ ,  $3s < 3p < 3d$ ,  $2s < 2p$
- If Value of  $\ell$  is same but value of  $n$  is different then the order of energy will be.  
**Ex.**  $1s < 2s < 3s < 4s < 5s < 6s$   
 $3d < 4d < 5d < 6d$   
 $4p < 5p < 6p$
- The orbital angular momentum =  $\sqrt{\ell(\ell+1)} \frac{h}{2\pi}$  or  $\sqrt{\ell(\ell+1)} \hbar$   $\left\{ \because \hbar = \frac{h}{2\pi} \right\}$  {  $\hbar$  is called as 'hash' }  
 Orbital angular momentum : For s subshell = 0  
 For p subshell =  $\sqrt{2} \frac{h}{2\pi}$  or  $\sqrt{2} \hbar$
- The number of electrons in a particular subshell is equal to  $2(2\ell + 1)$   
 for s subshell number of electrons =  $2 e^-$   
 for p subshell number of electrons =  $6 e^-$   
 for d subshell number of electrons =  $10 e^-$   
 for f subshell number of electrons =  $14 e^-$
- Shape of the orbital :  

s	→	spherical
p	→	dumb bell shape
d	→	double dumb bell shape
f	→	complex shape



## BEGINNER'S BOX-5

1. de-Broglie wavelength is related to applied voltage as :-  
 (1)  $\lambda = \frac{12.3}{\sqrt{h}} \text{ \AA}$       (2)  $\lambda = \frac{12.3}{\sqrt{V}} \text{ \AA}$       (3)  $\lambda = \frac{12.3}{\sqrt{r}} \text{ \AA}$       (4)  $\lambda = \frac{12.3}{\sqrt{m}} \text{ \AA}$
2. Select the incorrect statements among the following.  
 (1)  $\Delta x \cdot \Delta p \geq \frac{h}{4\pi}$       (2)  $\Delta x \cdot \Delta p \geq \frac{h}{4\pi m}$       (3)  $\Delta x \cdot \Delta V \geq \frac{h}{4\pi m}$       (4)  $\Delta E \cdot \Delta t \geq \frac{h}{4\pi}$
3. If the kinetic energy of an electron is increased 4 times, the wavelength of the de-Broglie wave associated with it would become :-  
 (1) four times      (2) two times      (3) half times      (4) one fourth times
4. Velocity of de-Broglie wave is given by :-  
 (1)  $\frac{c^2}{v}$       (2)  $\frac{h\nu}{mc}$       (3)  $\frac{mc^2}{h}$       (4)  $v\lambda$
5. The representation of an orbital with  $n = 4$  and  $\ell = 1$  :-  
 (1) 4d      (2) 4s      (3) 4f      (4) 4p
6. Maximum number of electrons present in M shell is :  
 (1) 8      (2) 18      (3) 32      (4) 10

**(c) Magnetic Quantum Number /Orientation Quantum Number (m) :**

Given by Linde

- It represents the orientation of electron cloud (orbital)
- Under the influence of magnetic field each subshell is further subdivided into orbitals (The electron cloud is known as orbital)  
Magnetic quantum number describes these different distributions of electron cloud.
- Value of  $m =$  all integral value from  $-\ell$  to  $+\ell$  including zero.  
i.e. Value of  $m = -\ell$  to  $+\ell$

**Orbital :** 3D space around the nucleus where the probability of finding electrons is maximum is called an orbital. An orbital can be represented by 3 set of quantum numbers

$$= \Psi_{n,\ell,m}$$

Ex. 1 :  $2p_x$ ;  $n=2, \ell=1, m=-1$  or  $m=+1$

Ex. 2 :  $3d_{z^2}$ ;  $n=3, \ell=2, m=0$

Ex. 3 :  $\Psi_{(3,2,0)}$ ;  $n=3, \ell=2, m=0$ ;  $3d_{z^2}$

**Node :** It is point /line / plane / surface in which probability of finding electron is zero.

$$\text{Total numbers of nodes} = \boxed{n-1}$$

They are of 2 types.

(i) Radial nodes / Spherical nodes / Nodal surface number of radial nodes =  $n-\ell-1$

(ii) Angular nodes / Nodal planes number of angular nodes / nodal planes =  $\ell$

\* Nucleus and  $\infty$  (infinite) are not considered as node.

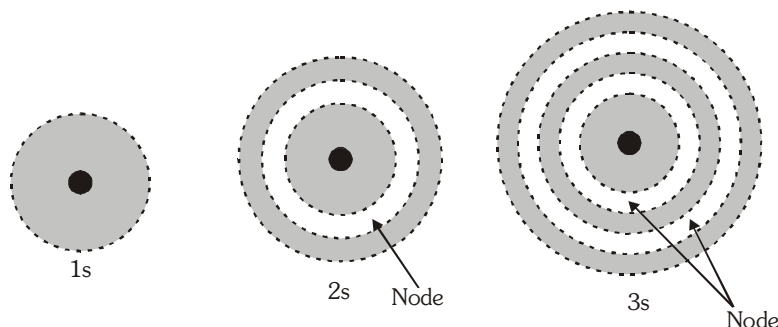


## Types of orbitals :

**Case-I :** If  $\ell = 0$  then  $m = 0$ , it implies that s subshell has only one orbital called as s orbital.

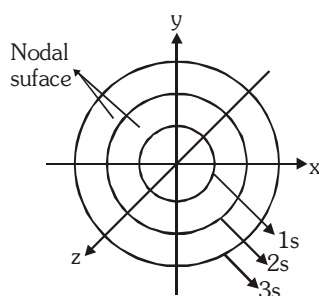
### Shapes of s-orbitals :

The s-orbitals are spherically symmetrical about the nucleus, i.e., the probability of finding electron is same in all directions from the nucleus. The size of the orbital depends on the value of principal quantum number. The 1s orbital is smaller than 2s-orbital and 2s-orbital is smaller than 3s, but all are spherical in shape as shown in figure.



Although the s-orbitals belonging to different shells are spherically symmetrical, yet they differ in certain respects as explained below :

- The probability of finding 1s electron is found to be maximum near the nucleus and decreases as the distance from the nucleus increases. In case of 2s electrons, the probability is again maximum near the nucleus and then decreases to zero as the distance from the nucleus increases. The intermediate region (a spherical shell) where the probability is zero is called a nodal surface or simply node. Thus, 2s-orbital differs from 1s-orbital in having one node within it. Similarly, 3s has two nodes. In general, any ns orbital has  $(n - 1)$  nodes.
- The size and energy of the s-orbital increases as the principal quantum number increases, i.e., the size and energy of s-orbital increases in the order  $1s < 2s < 3s \dots$



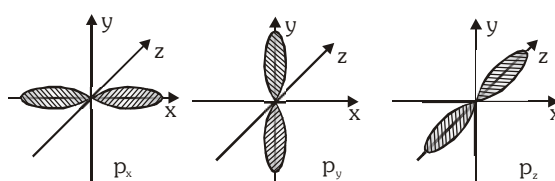
The s orbital of higher energy levels are also symmetrically spherical and can be represented as above

**Case-II** If  $\ell = 1$  ( p - subshell) then  $m = \begin{array}{c|c|c} -1 & 0 & +1 \\ \hline p_x & p_z & p_y \end{array}$

It implies that, p subshell have three orbitals called as  $p_x$ ,  $p_y$  and  $p_z$ .

### Shape of p-orbitals :

There are three p-orbitals, commonly referred to as  $p_x$ ,  $p_y$  and  $p_z$ . These three p-orbitals, possess equivalent energy and therefore, have same relation with the nucleus. They, however, differ in their direction & distribution of the charge.



These three p-orbitals are situated at right angle to one another and are directed along x, y and z axis (figure)

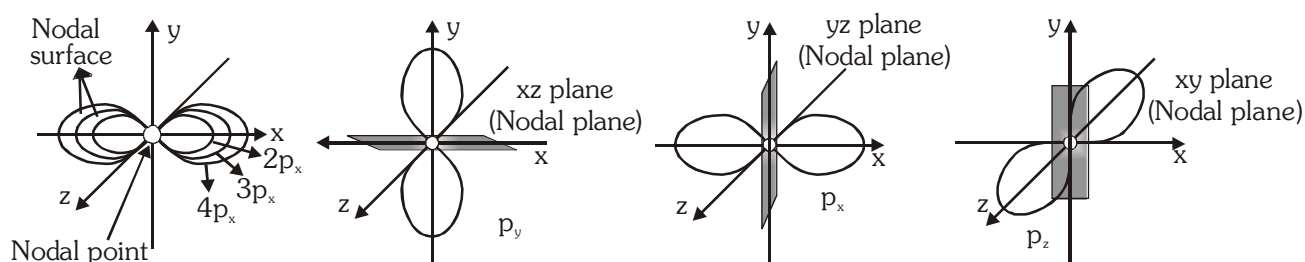
- Each p orbital has dumb bell shape ( 2 lobes which are separated from each other by a point of zero probability called nodal point or node or nucleus).
- The two lobes of each orbital are separated by a plane of zero electron density called nodal plane.
- Each p orbital of higher energy level are also dumb bell shape but they have nodal surface.

#### Nodal surface :

Orbital	Nodal surface
3 $p_x$	1
4 $p_x$	2
$np_x$	$(n - 2)$

#### Nodal Plane :

Orbital	Nodal plane
$p_x$	yz plane
$p_y$	xz plane
$p_z$	xy plane

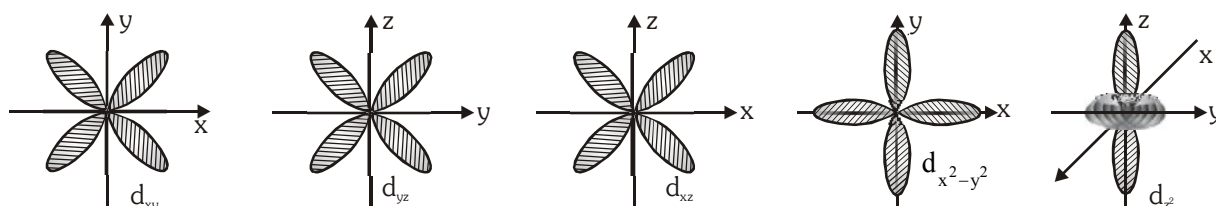


**Case III** When  $\ell = 2$ , 'm' has five values  $-2, -1, 0, +1, +2$ . It implies that d subshell of any energy shell has five orbitals. All the five orbitals are not identical in shape. Four of the d orbitals  $d_{xy}, d_{yz}, d_{xz}, d_{x^2-y^2}$  contain four lobes while fifth orbital  $d_{z^2}$  consists of only two lobes. The lobes of  $d_{xy}$  orbital lie between x and y axes. Similar is the case for  $d_{yz}$  and  $d_{xz}$ . Four lobes of  $d_{x^2-y^2}$  orbital are lying along x and y axes while the two lobes of  $d_{z^2}$  orbital are lying along z axis and contain a ring of negative charge surrounding the nucleus in xy plane. Geometry of d orbital is double dumbbell

$$m = \begin{matrix} & \text{---} & & & \text{---} & \\ & \text{---} & & & \text{---} & \\ -2 & -1 & 0 & +1 & +2 \\ \left| \begin{array}{c} d_{xy} \\ d_{yz} \\ d_{z^2} \\ d_{zx} \\ d_{x^2-y^2} \end{array} \right| \end{matrix}$$

#### Shape of d-orbitals :

It implies that d subshell has 5 orbitals i.e. five electron cloud and can be represented as follows

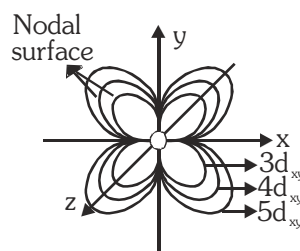


Each d-orbital of higher energy level also have double dumbbell shape but they have nodal surface.

#### In d-orbitals :

- Nodal Point  $\rightarrow 1$
- Nodal Surface  $\rightarrow$ 
  - 3  $d_{xy} \rightarrow 0$  Nodal surface
  - 4  $d_{xy} \rightarrow 1$  Nodal surface
  - 5  $d_{xy} \rightarrow 2$  Nodal surface
  - $n d_{xy} \rightarrow (n - 3)$

Number of nodal surface =  $n - \ell - 1$



- (iii) Nodal plane :  $d_{xy} \rightarrow xz \text{ \& } yz$  nodal plane :  
 $d_{xz} \rightarrow xy \text{ \& } zy$  nodal plane :  
 $d_{zy} \rightarrow zx \text{ \& } yx$  nodal plane :  
 $d_{x^2-y^2} \rightarrow 2$ , nodal plane :  
 $d_{z^2} \rightarrow 0$ , nodal plane :

**Note:** Orbitals of d subshell are equivalent in energy.

**(d) Spin Quantum number (s) :**

Given by **Goudsmit** and **Uhlenbeck**

- It represents the direction of electron spin around its own axis
- For clockwise spin/spin up( $\uparrow$ ) electron  $\rightarrow \pm \frac{1}{2}$
- For anti-clockwise spin/spin down( $\downarrow$ ) electron  $\rightarrow \mp \frac{1}{2}$

Spin angular momentum of an electron =  $\sqrt{s(s+1)} \cdot \frac{h}{2\pi}$  or  $\sqrt{s(s+1)} \hbar$

- Each orbital can accommodate 2 electrons with opposite spin or spin paired.

Correct  $\uparrow\downarrow$  Spin paired  $e^-$

Wrong  $\uparrow\uparrow$  Spin parallel  $e^-$

## Illustrations

**Illustration 41.** Calculate the value of n,  $\ell$  and m for  $7p_y$  orbital ?

**Solution**  $n = 7, \ell = 1, m = +1 \text{ or } -1$

**Illustration 42.** Calculate the value of n,  $\ell$  and m for 3s orbital ?

**Solution**  $n = 3, \ell = 0, m = 0$

**Illustration 43.** Calculate the value of n,  $\ell$  and m for  $5d_{z^2}$  orbital ?

**Solution**  $n = 5, \ell = 2, m = 0$

**Illustration 44.** Which of the following set of quantum numbers is not possible ?

(a)  $n = 2, \ell = 0, m = -1, s = -\frac{1}{2}$

(b)  $n = 3, \ell = 2, m = 0, s = \pm \frac{1}{2}$

(c)  $n = 2, \ell = 3, m = -2, s = \pm \frac{1}{2}$

**Solution** (a) not possible (b) possible (c) not possible



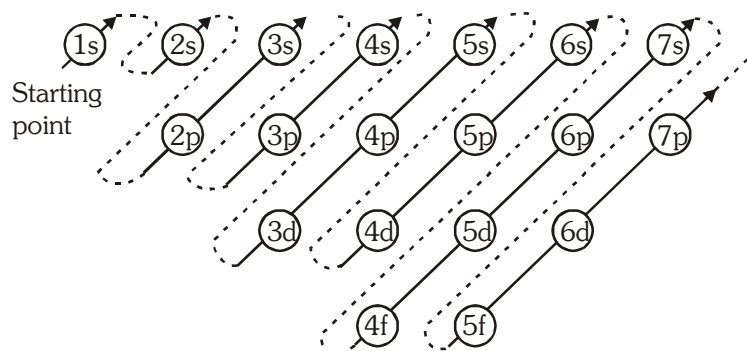
## 2.11 RULES FOR FILLING OF ELECTRONS

- (a) Aufbau Principle (b)  $(n + \ell)$  rule  
(c) Hund's maximum multiplicity principle (d) Pauli's exclusion principle

### (a) Aufbau Principle

Aufbau is a German word and its meaning is 'Building up'

- Aufbau principle gives a sequence in which various subshell are filled up depending on the relative order of the energies of various subshell.
- Principle : The subshell with minimum energy is filled up first when this subshell obtained maximum quota of electrons then the next subshell of higher energy starts filling.
- The sequence in which various subshell are filled are as follows.



$1s^2, 2s^2, 2p^6, 3s^2, 3p^6, 4s^2, 3d^{10}, 4p^6, 5s^2, 4d^{10}, 5p^6, 6s^2, 4f^{14}, 5d^{10}, 6p^6, 7s^2, 5f^{14}, 6d^{10}, \dots$

### For Example

${}^1\text{H}$	$\rightarrow$	$1s^1$
${}^2\text{He}$	$\rightarrow$	$1s^2$
${}^3\text{Li}$	$\rightarrow$	$1s^2, 2s^1$
${}^4\text{Be}$	$\rightarrow$	$1s^2, 2s^2$
${}^5\text{B}$	$\rightarrow$	$1s^2, 2s^2, 2p^1$
${}^6\text{C}$	$\rightarrow$	$1s^2, 2s^2, 2p^2$
${}^7\text{N}$	$\rightarrow$	$1s^2, 2s^2, 2p^3$
${}^8\text{O}$	$\rightarrow$	$1s^2, 2s^2, 2p^4$
${}^9\text{F}$	$\rightarrow$	$1s^2, 2s^2, 2p^5$
${}^{10}\text{Ne}$	$\rightarrow$	$1s^2, 2s^2, 2p^6$
${}^{11}\text{Na}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^1$
${}^{12}\text{Mg}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2$
${}^{13}\text{Al}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^1$
${}^{14}\text{Si}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^2$
${}^{15}\text{P}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^3$
${}^{16}\text{S}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^4$
${}^{17}\text{Cl}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^5$
${}^{18}\text{Ar}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^6$
${}^{19}\text{K}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^6, 4s^1$
${}^{20}\text{Ca}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^6, 4s^2$
${}^{21}\text{Sc}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^6, 4s^2, 3d^1$
${}^{22}\text{Ti}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^6, 4s^2, 3d^2$
${}^{23}\text{V}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^6, 4s^2, 3d^3$
${}^{24}\text{Cr}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^6, 4s^1, 3d^5$ [Exception]
${}^{25}\text{Mn}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^6, 4s^2, 3d^5$
${}^{26}\text{Fe}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^6, 4s^2, 3d^6$
${}^{27}\text{Co}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^6, 4s^2, 3d^7$
${}^{28}\text{Ni}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^6, 4s^2, 3d^8$
${}^{29}\text{Cu}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^6, 4s^1, 3d^{10}$ [Exception]
${}^{30}\text{Zn}$	$\rightarrow$	$1s^2, 2s^2, 2p^6, 3s^2, 3p^6, 4s^2, 3d^{10}$



**Electronic configuration can be written by following different methods :**

- ${}_{26}\text{Fe} \rightarrow$ 
  - $1s^2, 2s^2, 2p^6, 3s^2, 3p^6, 4s^2, 3d^6$
  - $1s^2, 2s^2, 2p^6, 3s^2, 3p^6, 3d^6, 4s^2$
  - $1s^2, 2s^2p^6, 3s^2p^6d^6, 4s^2$
  - $$\begin{array}{cccc} 2 & 8 & 14 & 2 \\ (4) & [\text{Ar}] & 4s^2 & 3d^6 \end{array}$$

- ${}_{26}\text{Fe} \rightarrow$ 

$$1s^2 \underbrace{2s^2 2p^6}_{(n-2)} \underbrace{3s^2 3p^6 3d^6}_{(n-1)} \underbrace{4s^2}_n$$

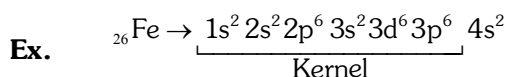
$n \rightarrow$  Outer most Shell or Ultimate Shell or Valence Shell

In this Shell electrons are called as Valence electrons or this is called core charge

$(n-1) \rightarrow$  Penultimate Shell or core or pre valence Shell

$(n-2) \rightarrow$  Pre Penultimate Shell

- If we remove the last 'n' Shell (ultimate Shell) then the remaining shells are collectively called as Kernel.



### (b) $(n + \ell)$ Rule (For multi electron species)

According to it the sequence in which various subshell are filled up can also be determined with the help of  $(n + \ell)$  value for a given subshell.

#### Principle of $(n + \ell)$ rule :

The subshell with lowest  $(n + \ell)$  value is filled up first. When two or more subshell have same  $(n + \ell)$  value then the subshell with lowest value of  $n$  is filled up first.

#### In case of H-atom :

Energy only depends on principal quantum number

$$1s < 2s = 2p < 3s = 3p = 3d < 4s = 4p = 4d = 4f < \dots\dots\dots$$

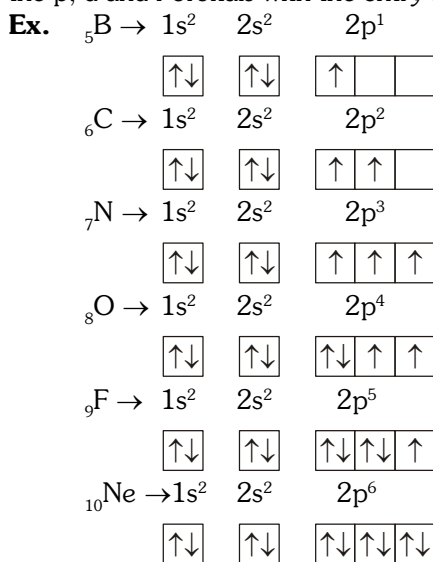
Sub Shell	n	$\ell$	$n + \ell$	
1s	1	0	1	
2s	2	0	2	
2p	2	1	3	(1)
3s	3	0	3	(2)
3p	3	1	4	(1)
4s	4	0	4	(2)
3d	3	2	5	(1)
4p	4	1	5	(2)
5s	5	0	5	(3)
4d	4	2	6	(1)
5p	5	1	6	(2)
6s	6	0	6	(3)

**Order :**  $1s^2, 2s^2, 2p^6, 3s^2, 3p^6, 4s^2, 3d^{10}, 4p^6, 5s^2, 4d^{10}, 5p^6, 6s^2, 4f^{14}, 5d^{10}, 6p^6, 7s^2, 5f^{14}, 6d^{10}, \dots$



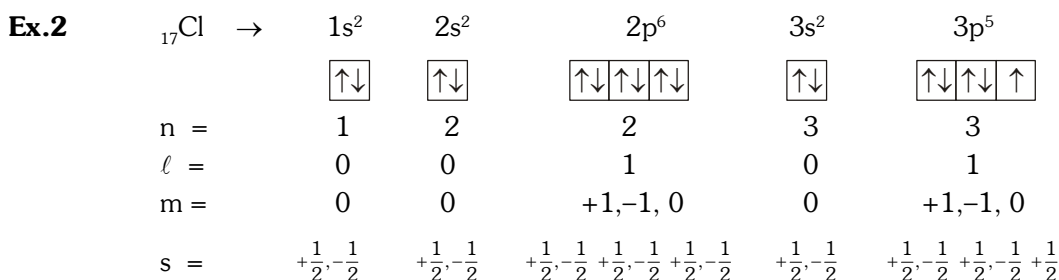
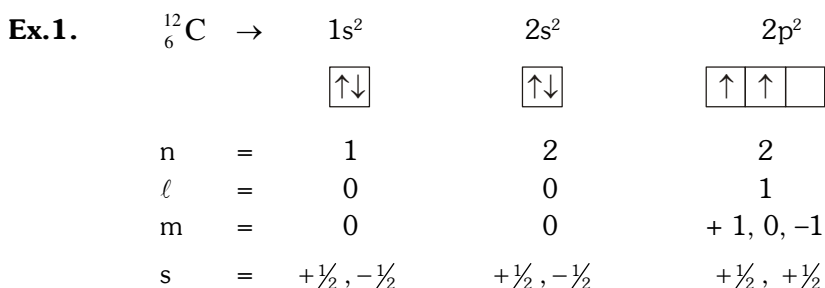
(c) **Hund's Maximum Multiplicity Rule** (Multiplicity : Many of the same kind)

- This rule deals with the filling of electrons into the orbitals belonging to the same subshell (that is, orbitals of equal energy, called degenerate orbitals).
- It states : pairing of electrons in the orbitals belonging to the same subshell (p, d or f) does not take place until each orbital belonging to that subshell has got one electron each i.e., it is singly occupied.
- Since there are three p, five d and seven f orbitals, therefore, the pairing of electrons will start in the p, d and f orbitals with the entry of 4th, 6th and 8th electron, respectively.



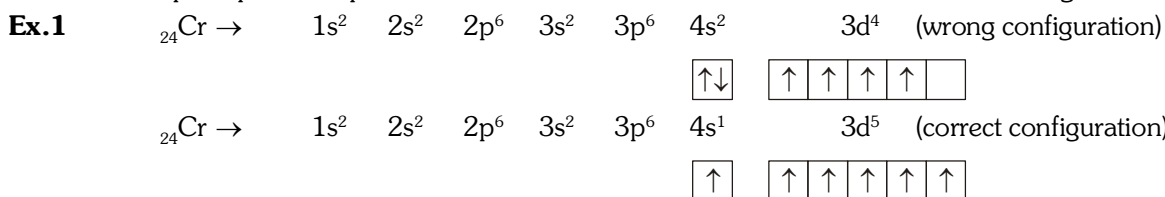
(d) **Pauli's Exclusion Principle**

In 1925 Pauli stated that no two electron in an atom can have same values of all four quantum numbers i.e., an orbital can accommodate maximum 2 electrons with opposite spin.

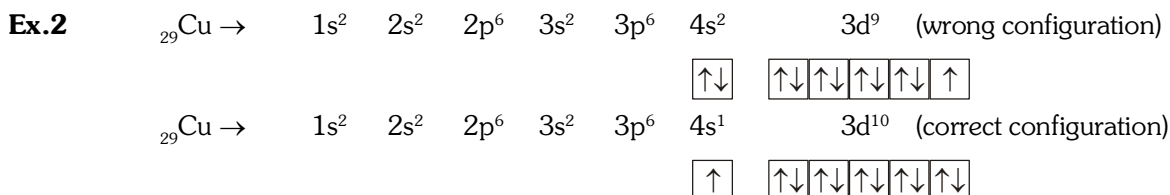


**Exception of Aufbau principle :**

In some cases it is seen that the electronic configuration is slightly different from the arrangement given by Aufbau principle. A simple reason behind this is that half filled & full filled subshell have got extra stability.







## Illustrations

**Illustration 45.** Calculate the number of unpaired electrons in Cr

**Solution**  $_{24}\text{Cr} \rightarrow 1s^2 2s^2 2p^6 3s^2 3p^6 4s^1 3d^5$   
 in  $_{24}\text{Cr}$ , 6 electrons are unpaired.

**Illustration 46.** The number of unpaired electrons in  $\text{Cr}^{+3}$

**Solution**  $\text{Cr}^{+3} \rightarrow 1s^2 2s^2 2p^6 3s^2 3p^6 4s^0 3d^3$   
 in  $\text{Cr}^{+3}$ , 3 electrons are unpaired.

**Illustration 47.** The number of unpaired electrons in 3d subshell of  $\text{Cr}^{+3}$

**Solution** 3

**Illustration 48.** The number of unpaired electrons in  $\text{Fe}^{+2}$  &  $\text{Fe}^{+3}$

**Solution**  $\text{Fe}^{+2} \rightarrow 1s^2 2s^2 2p^6 3s^2 3p^6 4s^0 3d^6 = 4$  unpaired electrons  
 $\text{Fe}^{+3} \rightarrow 1s^2 2s^2 2p^6 3s^2 3p^6 4s^0 3d^5 = 5$  unpaired electrons

### BEGINNER'S BOX-6

- A neutral atom of an element has 2K, 8L, 11 M and 2N electrons. The number of p-electrons in the atom are :-  
 (1) 2 (2) 12 (3) 10 (4) 6
- An atom has 2 electrons in K-shell, 8 electrons in L-shell & 8 electrons in M-shell. The number of p-electrons presents in the element is :-  
 (1) 10 (2) 7 (3) 12 (4) 4
- The maximum number of such electrons in an atom with quantum number  $n = 3$ ,  $\ell = 2$  is :-  
 (1) 2 (2) 6 (3) 10 (4) 14
- The number of orbitals in  $n=3$  are :-  
 (1) 1 (2) 4 (3) 9 (4) 16
- In potassium the probable order of energy level for 19<sup>th</sup> electron is :-  
 (1)  $3s > 3d$  (2)  $4s < 3d$  (3)  $4s > 4p$  (4)  $4s = 3d$

## ANSWER KEY

<b>BEGINNER'S BOX-1</b>	<b>Que.</b>	1	2	3	4	5	6	7			
	<b>Ans.</b>	3	3	2	4	4	4	2			
<b>BEGINNER'S BOX-2</b>	<b>Que.</b>	1	2	3	4						
	<b>Ans.</b>	3	1	2	1						
<b>BEGINNER'S BOX-3</b>	<b>Que.</b>	1	2	3	4	5	6				
	<b>Ans.</b>	3	4	3	2	2	3				
<b>BEGINNER'S BOX-4</b>	<b>Que.</b>	1	2	3	4						
	<b>Ans.</b>	3	3	2	2						
<b>BEGINNER'S BOX-5</b>	<b>Que.</b>	1	2	3	4	5	6				
	<b>Ans.</b>	2	2	3	2	4	2				
<b>BEGINNER'S BOX-6</b>	<b>Que.</b>	1	2	3	4	5					
	<b>Ans.</b>	2	3	3	3	2					



**EXERCISE-I (Conceptual Questions)****INTRODUCTION**

- Rutherford's  $\alpha$ -particle scattering experiment proved that atom has :-  
 (1) Electrons (2) Neutrons  
 (3) Nucleus (4) Orbitals
- A and B are two elements which have same atomic weight and are having atomic number 27 and 30 respectively. If the atomic weight of A is 57 then number of neutron in B is :-  
 (1) 27 (2) 33 (3) 30 (4) 40
- Find out the atoms which are isoneutronic :-  
 (1)  $^{14}_6\text{C}$ ,  $^{15}_7\text{N}$ ,  $^{17}_9\text{F}$  (2)  $^{12}_6\text{C}$ ,  $^{14}_7\text{N}$ ,  $^{19}_9\text{F}$   
 (3)  $^{14}_6\text{C}$ ,  $^{14}_7\text{N}$ ,  $^{17}_9\text{F}$  (4)  $^{14}_6\text{C}$ ,  $^{14}_7\text{N}$ ,  $^{19}_9\text{F}$
- Species which are isoelectronic to one another are  
 (a)  $\text{CN}^-$  (b)  $\text{OH}^-$   
 (c)  $\text{CH}_3^+$  (d)  $\text{N}_2$   
 (e) CO  
 Correct answer is :-  
 (1) a, b, c (2) a, c, d  
 (3) a, d, e (4) b, c, d
- For any anion  $\text{X}^{-3}$ , the mass number is 14. If anion has 10 electrons, then number of neutrons in  $\text{X}_2$  nucleus :-  
 (1) 10 (2) 14  
 (3) 7 (4) 5
- Which of the following pairs is correctly matched :  
 (1) Isotopes  $^{40}_{20}\text{Ca}$ ,  $^{40}_{19}\text{K}$   
 (2) Isotones  $^{30}_{14}\text{Si}$ ,  $^{31}_{15}\text{P}$ ,  $^{32}_{16}\text{S}$   
 (3) Isobars  $^{16}_8\text{O}$ ,  $^{17}_8\text{O}$ ,  $^{18}_8\text{O}$   
 (4) Isoelectronic  $\text{N}^{-3}$ ,  $\text{O}^{-2}$ ,  $\text{Cr}^{+3}$
- The atom A, B, C have the configuration  
 $\text{A} \rightarrow [\text{Z}(90) + n(146)]$ ,  $\text{B} \rightarrow [\text{Z}(92) + n(146)]$ ,  
 $\text{C} \rightarrow [\text{Z}(90) + n(148)]$  So that :-  
 (a) A and C - Isotones (b) A and C - Isotopes  
 (c) A and B - Isobars (d) B and C - Isobars  
 (e) B and C - Isotopes  
 The wrong statements are:-  
 (1) a, b only (2) c, d, e only  
 (3) a, c, d only (4) a, c, e only

- (i)  $^{54}_{26}\text{Fe}$ ,  $^{56}_{26}\text{Fe}$ ,  $^{57}_{26}\text{Fe}$ ,  $^{58}_{26}\text{Fe}$  (a) Isotopes  
 (ii)  $^3_1\text{H}$ ,  $^3_2\text{He}$  (b) Isotones  
 (iii)  $^{76}_{32}\text{Ge}$ ,  $^{77}_{33}\text{As}$  (c) Isodiaphers  
 (iv)  $^{235}_{92}\text{U}$ ,  $^{231}_{90}\text{Th}$  (d) Isobars  
 (v)  $^1_1\text{H}$ ,  $^2_1\text{D}$ ,  $^3_1\text{T}$

Match the above correct terms:-

- (1) [(i), - a], [(ii) - d], [(iii) - b], [(iv) - c], [(v) - a]  
 (2) [(i) - a] [(ii) - d], [(iii) - d] [(iv) - c] [v - a]  
 (3) [v - a] [(iv) - c]. [(iii) - d] [(ii) - b] [(i) - a]  
 (4) None of them
- Choose the false statement about deuterium :-  
 (1) It is an isotope of hydrogen  
 (2) It contains [(1 e) + (1 p) + (1 n)]  
 (3) It contains only [(1 p) + (1 n)]  
 (4)  $\text{D}_2\text{O}$  is called as heavy water
- If the table of atomic masses is established with the oxygen atom and assigned value of 200, then the mass of carbon atom would be, approximately:-  
 (1) 24 (2) 150 (3) 50 (4) 112
- The relative abundance of two rubidium isotopes of atomic weights 85 and 87 are 75% and 25% respectively. The average atomic weight of rubidium is:-  
 (1) 75.5 (2) 85.5 (3) 86.5 (4) 87.5
- The ratio of specific charge of a proton and an  $\alpha$ -particle is :-  
 (1) 2 : 1 (2) 1 : 2 (3) 1 : 4 (4) 1 : 1
- In an atom  $^{27}_{13}\text{Al}$ , number of proton is (a), electron is (b) and neutron is (c). Hence ratio will be [in order c : b : a] :-  
 (1) 13 : 14 : 13 (2) 13 : 13 : 14  
 (3) 14 : 13 : 13 (4) 14 : 13 : 14
- Atomic weight of Ne is 20.2. Ne is mixture of  $^{20}\text{Ne}$  and  $^{22}\text{Ne}$ , relative abundance of heavier isotope is :-  
 (1) 90 (2) 20 (3) 40 (4) 10
- Number of protons, neutrons & electrons in the element  $^{231}_{89}\text{Y}$  is :-  
 (1) 89, 231, 89 (2) 89, 89, 242  
 (3) 89, 142, 89 (4) 89, 71, 89



16. Atoms  $^{13}_6\text{C}$  and  $^{17}_8\text{O}$  are related to each other as:-  
 (1) Isotones (2) Isoelectronic  
 (3) Isodiaphers (4) Isosters
17. The  $e/m$  ratio is maximum for :-  
 (1)  $\text{D}^+$  (2)  $\text{He}^+$  (3)  $\text{H}^+$  (4)  $\text{He}^{2+}$
18. Let mass of electron is half, mass of proton is two times and mass of neutron is three fourth of original masses, then new atomic weight of  $^{16}\text{O}$  atom:-  
 (1) increases by 37.5 %  
 (2) remain constant  
 (3) increases by 12.5 %  
 (4) decreases by 25 %
19. An isotone of  $^{76}_{32}\text{Ge}$  is :-  
 (i)  $^{77}_{32}\text{Ge}$  (ii)  $^{77}_{33}\text{As}$   
 (iii)  $^{77}_{34}\text{Se}$  (iv)  $^{78}_{34}\text{Se}$   
 (1) (ii) & (iii) (2) (i) & (ii)  
 (3) (ii) & (iv) (4) (ii) & (iii) & (iv)
20. In  $^{14}_7\text{N}$  if mass attributed to electrons were doubled & the mass attributed to protons were halved, the atomic mass would become approximately :-  
 (1) Halved  
 (2) Doubled  
 (3) Reduced by 25%  
 (4) Remain same
21. The value of planck's constant is  $6.63 \times 10^{-34}\text{Js}$ . The velocity of light is  $3.0 \times 10^8\text{ms}^{-1}$ . Which value is closest to the wavelength in metres of a quantum of light with frequency of  $8 \times 10^{15}\text{s}^{-1}$ ?  
 (1)  $3 \times 10^{-7}$  (2)  $2 \times 10^{-25}$   
 (3)  $5 \times 10^{-18}$  (4)  $3.75 \times 10^{-8}$
22. If change in energy ( $\Delta E$ ) =  $3 \times 10^{-8}\text{J}$ ,  $h = 6.64 \times 10^{-34}\text{J-s}$  and  $c = 3 \times 10^8\text{m/s}$ , then wavelength of the light is :-  
 (1)  $6.64 \times 10^3\text{\AA}$  (2)  $6.64 \times 10^5\text{\AA}$   
 (3)  $6.64 \times 10^{-8}\text{\AA}$  (4)  $6.64 \times 10^{18}\text{\AA}$

### BOHR'S ATOMIC MODEL

23. Angular momentum in second Bohr orbit of H-atom is x. Then find out angular momentum in 1st excited state of  $\text{Li}^{+2}$  ion :  
 (1)  $3x$  (2)  $9x$  (3)  $\frac{x}{2}$  (4)  $x$
24. Angular momentum for P-shell electron is :-  
 (1)  $\frac{3h}{\pi}$  (2) Zero (3)  $\frac{\sqrt{2}h}{2\pi}$  (4) None

25. Multiplication of electron velocity and radius for a orbit in an atom is :-  
 (1) Proportional to mass of electron  
 (2) Proportional to square of mass of electron  
 (3) Inversely proportional to mass of electron  
 (4) Does not depend upon mass of electron
26. The radius of a shell for H-atom is  $4.761\text{\AA}$ . The value of n is :-  
 (1) 3 (2) 9 (3) 5 (4) 4
27. In Bohr's atomic model radius of 1<sup>st</sup> orbit of Hydrogen is  $0.053\text{ nm}$  then radius of 3<sup>rd</sup> orbit of  $\text{Li}^{+2}$  is :  
 (1) 0.159 (2) 0.053  
 (3) 0.023 (4) 0.026
28. The first three radius ratio of Bohr orbits :-  
 (1) 1 : 0.5 : 0.5 (2) 1 : 2 : 3  
 (3) 1 : 4 : 9 (4) 1 : 8 : 27
29. For  $\text{Li}^{+2}$  ion,  $r_2 : r_5$  will be :-  
 (1) 9 : 25 (2) 4 : 25 (3) 25 : 4 (4) 25 : 9
30. The ratio of the radii of two Bohr orbits of H-atom is 4 : 1, what would be their nomenclature :-  
 (1) K & L (2) L & K  
 (3) N & L (4) 2 & 3 both
31. The velocity of electron in third excited state of  $\text{Be}^{3+}$  ion will be :-  
 (1)  $\frac{3}{4}(2.188 \times 10^8)\text{ms}^{-1}$  (2)  $\frac{3}{4}(2.188 \times 10^6)\text{ms}^{-1}$   
 (3)  $(2.188 \times 10^6)\text{Kms}^{-1}$  (4)  $(2.188 \times 10^3)\text{Kms}^{-1}$
32. The Bohr orbit radius for the hydrogen atom ( $n = 1$ ) is approximately  $0.530\text{\AA}$ . The radius for the first excited state ( $n = 2$ ) will be :-  
 (1)  $0.13\text{\AA}$  (2)  $1.0\text{\AA}$  (3)  $4.77\text{\AA}$  (4)  $2.12\text{\AA}$
33. According to Bohr theory, the radius (r) and velocity (v) of an electron vary with the increasing principal quantum number 'n' as :-  
 (1) r increases, v decreases  
 (2) r and v both increases  
 (3) r & v both decreases  
 (4) r decreases, v increases
34. The ratio of radius of first orbit in hydrogen to the radius of first orbit in deuterium will be :-  
 (1) 1 : 1 (2) 1 : 2 (3) 2 : 1 (4) 4 : 1



35. For any H like system, the ratio of velocities of I, II & III orbit i.e.,  $V_1 : V_2 : V_3$  will be :-

- (1) 1 : 2 : 3                      (2) 1 : 1/2 : 1/3  
(3) 3 : 2 : 1                      (4) 1 : 1 : 1

36. The energy of H-atom in  $n^{\text{th}}$  orbit is  $E_n$ , then energy in  $n^{\text{th}}$  orbit of singly ionised helium atom will be:-

- (1)  $4E_n$                               (2)  $E_n/4$   
(3)  $2E_n$                               (4)  $E_n/2$

37. The energy of second Bohr orbit of the hydrogen atom is  $-328 \text{ kJ/mol}$ . Hence the energy of fourth Bohr orbit should be :

- (1)  $-41 \text{ kJ/mol}$   
(2)  $-1312 \text{ kJ/mol}$   
(3)  $-164 \text{ kJ/mol}$   
(4)  $-82 \text{ kJ/mol}$

38. In a hydrogen atom, if energy of an electron in ground state is  $-13.6 \text{ eV}$ , then energy in the  $2^{\text{nd}}$  excited state is :-

- (1)  $-1.51 \text{ eV}$                       (2)  $-3.4 \text{ eV}$   
(3)  $-6.04 \text{ eV}$                       (4)  $-13.6 \text{ eV}$

39. The ratio between kinetic energy and the total energy of the electron of hydrogen atom according to Bohr's model is :-

- (1) 2 : 1                              (2) 1 : 1  
(3) 1 : -1                              (4) 1 : 2

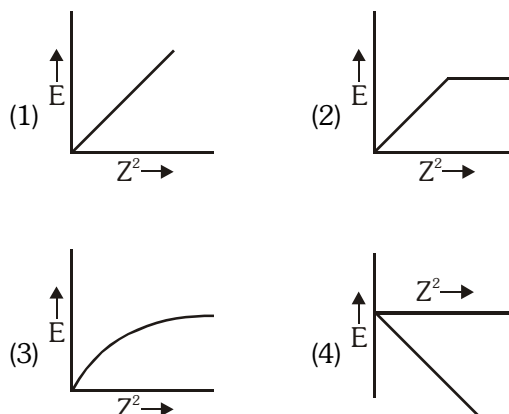
40. Potential energy is  $-27.2 \text{ eV}$  in second orbit of  $\text{He}^+$ , then calculate double of total energy in first excited state of hydrogen atom :-

- (1)  $-13.6 \text{ eV}$   
(2)  $-54.4 \text{ eV}$   
(3)  $-6.8 \text{ eV}$   
(4)  $-27.2 \text{ eV}$

41. The energy levels for  ${}_Z\text{A}^{(+Z-1)}$  can be given by :-

- (1)  $E_n$  for  $\text{A}^{(+Z-1)} = Z^2 \times E_n$  for H  
(2)  $E_n$  for  $\text{A}^{(+Z-1)} = Z \times E_n$  for H  
(3)  $E_n$  for  $\text{A}^{(+Z-1)} = \frac{1}{Z^2} \times E_n$  for H  
(4)  $E_n$  for  $\text{A}^{(+Z-1)} = \frac{1}{Z} \times E_n$  for H

42. The graphical representation of energy of electron and atomic number is :-



43. Going from K-shell to N-shell in case of H-atom :-

- (1) Kinetic energy decreases  
(2) Total energy decreases  
(3) Potential energy decreases  
(4) None of these

44. Maximum frequency of emission is obtained for the transition :-

- (1)  $n = 2$  to  $n = 1$                       (2)  $n = 6$  to  $n = 2$   
(3)  $n = 1$  to  $n = 2$                       (4)  $n = 2$  to  $n = 6$

45. If the ionization energy of hydrogen is  $313.8 \text{ kcal per mole}$ , then the energy of the electron in  $2^{\text{nd}}$  excited state will be :-

- (1)  $-113.2 \text{ kcal/mole}$                       (2)  $-78.45 \text{ kcal/mole}$   
(3)  $-313.8 \text{ kcal/mole}$                       (4)  $-35 \text{ kcal/mole}$

46. Which of the following electron transition will require the largest amount of energy in a hydrogen atom :-

- (1) From  $n = 1$  to  $n = 2$                       (2) From  $n = 2$  to  $n = 3$   
(3) From  $n = \infty$  to  $n = 1$                       (4) From  $n = 3$  to  $n = 5$

47. If the potential energy (PE) of hydrogen electron is  $-3.02 \text{ eV}$  then in which of the following excited level is electron present :-

- (1)  $1^{\text{st}}$                       (2)  $2^{\text{nd}}$                       (3)  $3^{\text{rd}}$                       (4)  $4^{\text{th}}$

48. The radiation of low frequency will be emitted in which transition of hydrogen atom :-

- (1)  $n = 1$  to  $n = 4$                       (2)  $n = 2$  to  $n = 5$   
(3)  $n = 3$  to  $n = 1$                       (4)  $n = 5$  to  $n = 2$

49. A single electron orbits a stationary nucleus ( $z = 5$ ). The energy required to excite the electron from third to fourth Bohr orbit will be :-

- (1)  $4.5 \text{ eV}$                               (2)  $8.53 \text{ eV}$   
(3)  $25 \text{ eV}$                               (4)  $16.53 \text{ eV}$



50. The ratio of energies of hydrogen atom for first and second excited state is :-  
 (1)  $4/1$  (2)  $1/4$  (3)  $4/9$  (4)  $9/4$
51.  $E_n = -313.6/n^2$ . If the value of  $E_n = -34.84$  then to which of the following values does 'n' correspond :-  
 (1) 1 (2) 2 (3) 3 (4) 4
52. The ratio of potential energy and total energy of an electron in a Bohr orbit of hydrogen like species is :-  
 (1) 2 (2) -2 (3) 1 (4) -1
53. Which is not a correct order of energy for 1, 2<sup>nd</sup> & 3<sup>rd</sup> orbit :-  
 (1)  $E_1 > E_2 > E_3$   
 (2)  $(PE)_1 < (PE)_2 < (PE)_3$   
 (3)  $(KE)_1 > (KE)_2 > (KE)_3$   
 (4) '1' & '3' both
54. Which of the following is a correct relationship :-  
 (1)  $E_1$  of H =  $1/2 E_2$  of  $He^+$  =  $1/3 E_3$  of  $Li^{+2}$  =  $1/4 E_4$  of  $Be^{+3}$   
 (2)  $E_1$  (H) =  $E_2$  ( $He^+$ ) =  $E_3$  ( $Li^{+2}$ ) =  $E_4$  ( $Be^{+3}$ )  
 (3)  $E_1$  (H) =  $2 E_2$  ( $He^+$ ) =  $3 E_3$  ( $Li^{+2}$ ) =  $4 E_4$  ( $Be^{+3}$ )  
 (4) No relation
55. Which is correct for any H like species :-  
 (1)  $(E_2 - E_1) > (E_3 - E_2) > (E_4 - E_3)$   
 (2)  $(E_2 - E_1) < (E_3 - E_2) < (E_4 - E_3)$   
 (3)  $(E_2 - E_1) = (E_3 - E_2) = (E_4 - E_3)$   
 (4)  $(E_2 - E_1) = 1/4 (E_3 - E_2) = 1/9 (E_4 - E_3)$
56. Which of the following is a correct graph :-
- (1)

(2)
- (3)

(4)
57. First excitation potential of H atom is :  
 (1) 10.2 eV (2) 3.4 eV  
 (3) 0 (4) - 3.4 eV
58. Energy required to remove an  $e^-$  from M shell of H-atom is 1.51 eV, then energy of first excited state will be :-  
 (1) -1.51 eV (2) +1.51 eV  
 (3) -3.4 eV (4) -13.6 eV

59. The ionisation potential of the hydrogen atom is 13.6 eV. The energy needed to ionise a hydrogen atom which is in its second excited state is about:-  
 (1) 13.6 eV (2) 10.2 eV  
 (3) 3.4 eV (4) 1.5 eV
60. The ionisation energy for excited hydrogen atom in eV will be :-  
 (1) 13.6 (2) Less than 13.6  
 (3) Greater than 13.6 (4) 3.4 or less
61. The energy required to excite an electron of H-atom from first orbit to second orbit is :-  
 (1)  $\frac{3}{4}$  of its ionisation energy  
 (2)  $\frac{1}{2}$  of its ionisation energy  
 (3)  $\frac{1}{4}$  of its ionisation energy  
 (4) None
62. The ionisation potential of a singly ionised helium ion is equivalent to :-  
 (1) Kinetic energy of first orbit  
 (2) Energy of last orbit  
 (3) Average energy in orbits  
 (4) Maximum energy in orbits
63. The ionisation energy for the H-atom is 13.6 eV, then the required energy to excite it from the ground state to next higher state will be :- (in eV)  
 (1) 3.4 (2) 10.2 (3) 12.1 (4) 1.5

### SPECTRUM AND SPECTRAL LINES

64. The spectrum of He is expected to be similar to that of :-  
 (1) H (2) Na  
 (3)  $He^+$  (4)  $Li^+$
65. Third line of Balmer series is produced by which transition in spectrum of H-atom  
 (1) 5 to 2 (2) 5 to 1  
 (3) 4 to 2 (4) 4 to 1
66. Which one of the following electron transitions between energy levels produces the line of shortest wavelength in hydrogen spectrum ?  
 (1)  $n_2 \rightarrow n_1$  (2)  $n_3 \rightarrow n_1$   
 (3)  $n_4 \rightarrow n_1$  (4)  $n_4 \rightarrow n_3$



67. Which series have highest energy in hydrogen spectrum :-  
 (1) Balmer (2) Brackett  
 (3) Pfund (4) Lyman
68. The ratio of minimum frequency of Lyman & Balmer series will be :-  
 (1) 1.25 (2) 0.25 (3) 5.4 (4) 10
69. Which transition emits photon of maximum frequency :-  
 (1) second spectral line of Balmer series  
 (2) second spectral line of Paschen series  
 (3) fifth spectral line of Humphery series  
 (4) first spectral line of Lyman series
70. Which one of the following species will give a series of spectral lines similar to that of  $\text{Mg}^{2+}$  :-  
 (1)  $\text{Al}^{3+}$  (2) Na (3)  $\text{Mg}^+$  (4) F
71. The ratio of minimum wavelengths of Lyman & Balmer series will be :-  
 (1) 1.25 (2) 0.25 (3) 5 (4) 10
72. The wavelength of photon obtained by electron transition between two levels in H-atom and singly ionised He are  $\lambda_1$  and  $\lambda_2$  respectively, then :-  
 (1)  $\lambda_2 = \lambda_1$  (2)  $\lambda_2 = 2\lambda_1$   
 (3)  $\lambda_2 = \lambda_1/2$  (4)  $\lambda_2 = \lambda_1/4$
73. Find out ratio of following for photon  
 $(\nu_{\text{max}})_{\text{Lyman}} : (\nu_{\text{max}})_{\text{Brackett}}$   
 (1) 1 : 16 (2) 16 : 1 (3) 4 : 1 (4) 1 : 4
74. The ratio of wavelengths of first line of Lyman series in  $\text{Li}^{+2}$  and first line of Lyman series in deuterium ( ${}^2_1\text{H}$ ) is :-  
 (1) 1 : 9 (2) 9 : 1 (3) 1 : 4 (4) 4 : 1
75. In an electronic transition atom cannot emit :-  
 (1) Visible light (2)  $\gamma$  - rays  
 (3) Infra red light (4) Ultra violet light
76. The first Lyman transition in the hydrogen spectrum has  $\Delta E = 10.2 \text{ eV}$ . The same energy change is observed in the second Balmer transition of :-  
 (1)  $\text{Li}^{2+}$  (2)  $\text{Li}^+$  (3)  $\text{He}^+$  (4)  $\text{Be}^{3+}$

77. The limiting line in Balmer series will have a frequency of :-  
 (1)  $3.65 \times 10^{14} \text{ sec}^{-1}$  (2)  $3.29 \times 10^{15} \text{ sec}^{-1}$   
 (3)  $8.22 \times 10^{14} \text{ sec}^{-1}$  (4)  $-8.22 \times 10^{14} \text{ sec}^{-1}$
78. If the shortest wavelength of Lyman series of H atom is x, then the wave length of first line of Balmer series of H atom will be :-  
 (1)  $\frac{9x}{5}$  (2)  $\frac{36x}{5}$  (3)  $\frac{5x}{9}$  (4)  $\frac{5x}{36}$
79. The first emission line in the H-atom spectrum in the Balmer series will have wave number :-  
 (1)  $\frac{5R}{36} \text{ cm}^{-1}$  (2)  $\frac{3R}{4} \text{ cm}^{-1}$   
 (3)  $\frac{7R}{144} \text{ cm}^{-1}$  (4)  $\frac{9R}{400} \text{ cm}^{-1}$
80. What transition in  $\text{He}^+$  will have the same  $\lambda$  as the I line in Lyman series of H - atom :-  
 (1)  $5 \rightarrow 3$  (2)  $3 \rightarrow 2$   
 (3)  $6 \rightarrow 4$  (4)  $4 \rightarrow 2$
81. In H-atom, electron transits from 6<sup>th</sup> orbit to 2<sup>nd</sup> orbit in multi step. Then total spectral lines (without Balmer series) will be :-  
 (1) 6 (2) 10 (3) 4 (4) 0
82. An atom has x energy level, then total number of lines in its spectrum are:-  
 (1)  $1 + 2 + 3 + \dots + (x-1)$   
 (2)  $1 + 2 + 3 + \dots + x^2$   
 (3)  $1 + 2 + 3 + \dots + (x-1)$   
 (4)  $(x+1)(x+2)(x+4)$
83. The figure indicates the energy level diagram for the origin of six spectral lines in emission spectrum (e.g. line no. 5 arises from the transition from level B to X) which of the following spectral lines will not occur in the absorption spectrum :-  
 (1) 1, 2, 3  
 (2) 3, 2  
 (3) 4, 5, 6  
 (4) 3, 2, 1
- 
84. A certain electronic transition from an excited state to ground state of the H atom in one or more step gives rise to three lines in the ultra violet region of the spectrum. How many lines does this transition produce in the infrared region of the spectrum :-  
 (1) 1 (2) 2 (3) 3 (4) 4





85. Four lowest energy levels of H-atom are shown in the figure. The number of emission lines could be :-
- |       |           |
|-------|-----------|
| (1) 3 | 4 _____   |
| (2) 4 | 3 _____   |
| (3) 5 | 2 _____   |
| (4) 6 | n=1 _____ |
86. In the above problem, the number of absorption lines could be :-
- (1) 3      (2) 4      (3) 5      (4) 6
87. If 9.9 eV energy is supplied to H atom, the no. of spectral lines emitted is equal to :-
- (1) 0      (2) 1      (3) 2      (4) 3

### DE-BROGLIE CONCEPT AND HEISENBERG PRINCIPLE

88. An electron has a kinetic energy of  $2.8 \times 10^{-23}$  J. de-Broglie wavelength will be nearly :-  
( $m_e = 9.1 \times 10^{-31}$  kg)
- (1)  $9.28 \times 10^{-24}$  m      (2)  $9.28 \times 10^{-7}$  m  
(3)  $9.28 \times 10^{-8}$  m      (4)  $9.28 \times 10^{-10}$  m
89. What is the de-Broglie wavelength associated with the hydrogen electron in its third orbit :-
- (1)  $9.96 \times 10^{-10}$  cm      (2)  $9.96 \times 10^{-8}$  cm  
(3)  $9.96 \times 10^4$  cm      (4)  $9.96 \times 10^8$  cm
90. If the de-Broglie wavelength of the fourth Bohr orbit of hydrogen atom is  $4\text{\AA}$ , the circumference of the orbit will be :-
- (1)  $4\text{\AA}$       (2) 4 nm      (3)  $16\text{\AA}$       (4) 16 nm
91. Number of waves in fourth orbit :-
- (1) 4      (2) 5      (3) 0      (4) 1
92. What is the ratio of the de-Broglie wavelengths for electrons accelerated through 200 volts and 50 volts :-
- (1) 1 : 2      (2) 2 : 1  
(3) 3 : 10      (4) 10 : 3
93. For a valid Bohr orbit, its circumference should be
- (1)  $= n\lambda$       (2)  $= (n-1)\lambda$   
(3)  $> n\lambda$       (4)  $< n\lambda$
94. A particle X moving with a certain velocity has a debroglie wavelength of  $1\text{\AA}$ . If particle Y has a mass of 25% that of X and velocity 75% that of X, de-Broglie wavelength of Y will be :-
- (1)  $3\text{\AA}$       (2)  $5.33\text{\AA}$   
(3)  $6.88\text{\AA}$       (4)  $48\text{\AA}$
95. The number of waves made by a Bohr electron in an orbit of maximum magnetic quantum number +2:-
- (1) 3      (2) 4      (3) 2      (4) 1
96. The uncertainty in position of an electron & helium atom are same. If the uncertainty in momentum for the electron is  $32 \times 10^5$ , then the uncertainty in momentum of helium atom will be
- (1)  $32 \times 10^5$       (2)  $16 \times 10^5$   
(3)  $8 \times 10^5$       (4) None
97. Calculate the uncertainty in the position of an electron (mass  $9.1 \times 10^{-28}$ g) moving with a velocity of  $3 \times 10^4$  cm sec<sup>-1</sup>, if the uncertainty in velocity is 0.011% ?
- (1) 1.92 cm      (2) 7.68 cm  
(3) 0.175 cm      (4) 3.84 cm
98. Heisenberg Uncertainty principle is not valid for
- (1) Moving electron      (2) Motor car  
(3) Stationary particles      (4) 2 & 3 both
99. What should be the momentum (in gram centimetre per second) of a particle if its de-Broglie wavelength is  $1\text{\AA}$  and the value of h is  $6.6252 \times 10^{-27}$  erg second ?
- (1)  $6.6252 \times 10^{-19}$  gcm/s  
(2)  $6.6252 \times 10^{-21}$  gcm/s  
(3)  $6.6252 \times 10^{-24}$  gcm/s  
(4)  $6.6252 \times 10^{-27}$  gcm/s
100. What should be the mass of the photon of sodium if its wavelength is  $5894\text{\AA}$ , the velocity of light is  $3 \times 10^8$  metre/second and the value of h is  $6.6252 \times 10^{-34}$  kg m<sup>2</sup>/s ?
- (1)  $3.746 \times 10^{-26}$  kg      (2)  $3.746 \times 10^{-30}$  kg  
(3)  $3.746 \times 10^{-34}$  kg      (4)  $3.746 \times 10^{-36}$  kg
101. Which of the following has least de-Broglie  $\lambda$  ?
- (1)  $e^-$       (2) p      (3)  $\text{CO}_2$       (4)  $\text{SO}_2$

### QUANTUM NUMBERS

102. The following quantum no. are possible for how many orbitals  $n = 3$ ,  $\ell = 2$ ,  $m = +2$  ?
- (1) 1      (2) 2      (3) 3      (4) 4
103. Number of possible orbitals (all types) in  $n = 3$  energy level is :-
- (1) 1      (2) 3      (3) 4      (4) 9
104. Which sub-shell is not permissible :-
- (1) 2d      (2) 4f      (3) 6p      (4) 3s



105. Nodal plane is found in which orbital :-

- (1)  $n = 2, \ell = 0$       (2)  $n = 3, \ell = 0$   
(3)  $n = 2, \ell = 1$       (4)  $n = 1, \ell = 0$

106. No. of nodal surface in 2s orbital :-

- (1) 0      (2) 1      (3) 2      (4) 3

107. Number of orbitals in h sub-shell is

- (1) 11      (2) 15      (3) 17      (4) 19

108. How many quantum numbers are required to specify the position of electron :-

- (1) 1      (2) 2      (3) 3      (4) 4

109. Which of the following is correct for a 4d-electron

(1)  $n = 4, \ell = 2, s = + \frac{1}{2}$

(2)  $n = 4, \ell = 2, s = 0$

(3)  $n = 4, \ell = 3, s = 0$

(4)  $n = 4, \ell = 3, s = + \frac{1}{2}$

110. If  $n = 3$ , then which value of ' $\ell$ ' is correct :-

- (1) 0      (2) 1  
(3) 2      (4) All of them

111. Energy of atomic orbitals in a particular shell is in order:-

- (1)  $s < p < d < f$       (2)  $s > p > d > f$   
(3)  $p < d < f < s$       (4)  $f > d > s > p$

112. Which statement is not correct for  $n = 5, m = 2$  :-

- (1)  $\ell = 4$   
(2)  $\ell = 0, 1, 2, 3; s = + 1/2$   
(3)  $\ell = 3$   
(4)  $\ell = 2, 3, 4$

113. Spin angular momentum for electron :-

- (1)  $\sqrt{s(s+1)} \frac{h}{2\pi}$       (2)  $\sqrt{2s(s+1)} \frac{h}{2\pi}$   
(3)  $\sqrt{s(s+2)} \frac{h}{2\pi}$       (4) None

114. The maximum number of electrons in a p-orbital with  $n = 6$  and  $m = 0$  can be :-

- (1) 14      (2) 6      (3) 2      (4) 10

115. The total number of value of  $m$  for the electrons in  $n = 4$  is -

- (1) 4      (2) 8      (3) 16      (4) 32

117. In an atom, for how many electrons, the quantum

numbers will be  $n = 3, \ell = 2, m = + 2, s = + \frac{1}{2}$  :-

- (1) 18      (2) 6      (3) 24      (4) 1

117. Which orbital is represented by the complete wave function  $\psi_{420}$  :-

- (1) 4d      (2) 3d      (3) 4p      (4) 4s

118. An electron is in one of 4d orbital. Which of the following orbital quantum number value is not possible :-

- (1)  $n = 4$       (2)  $\ell = 1$       (3)  $m = 1$       (4)  $m = 2$

119. A neutral atom of an element has 2K, 8L, 11M and 2N electrons. The number of s-electron in the atom are

- (1) 2      (2) 8      (3) 10      (4) 6

120. If  $\ell = 3$  then type and number of orbital is :-

- (1) 3p, 3      (2) 4f, 14      (3) 5f, 7      (4) 3d, 5

121. Any nf-orbital can accommodate upto :-

- (1) 14 electron  
(2) Six electrons  
(3) Two electrons with parallel spin  
(4) Two electrons with opposite spin

122.  $n, \ell$  and  $m$  values of an electron in  $3p_y$  orbital are :-

- (1)  $n = 3; \ell = 1$  and  $m = 1$   
(2)  $n = 3; \ell = 1$  and  $m = -1$   
(3) Both 1 and 2 are correct  
(4) None of these

123.  ${}_{36}\text{Kr}$  has the electronic configuration  $({}_{18}\text{Ar}) 4s^2 3d^{10} 4p^6$ . The 39<sup>th</sup> electron will go into which one of the following sub-levels :-

- (1) 4f      (2) 4d      (3) 3p      (4) 5s

124. The maximum probability of finding an electron in the  $d_{xy}$  orbital is :-

- (1) Along the x-axis  
(2) Along the y-axis  
(3) At an angle of  $45^\circ$  from the x and y axis  
(4) At an angle of  $90^\circ$  from the x and y axis

125. Which orbital has two angular nodal planes :-

- (1) s      (2) p      (3) d      (4) f

126. An orbital with  $\ell = 0$  is symmetrical about the :-

- (1) x-axis only      (2) y-axis only  
(3) z-axis only      (4) The nucleus





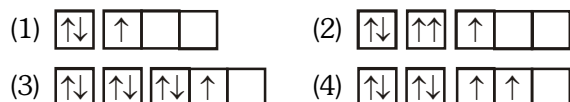
- 127.** If  $n$  &  $\ell$  are principal and azimuthal quantum no. respectively then the expression for calculating the total no. of electron in any energy level is :-

$$(1) \sum_{\ell=0}^{\ell=n} 2(2\ell+1) \quad (2) \sum_{\ell=1}^{\ell=n-1} 2(2\ell+1)$$

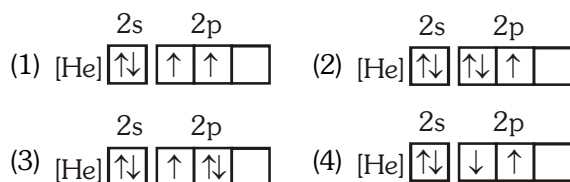
$$(3) \sum_{\ell=0}^{\ell=n+1} 2(2\ell+1) \quad (4) \sum_{\ell=0}^{\ell=n-1} 2(2\ell+1)$$

### RULES FOR FILLING OF ORBITALS

- 128.** Which configuration does not obey pauli's exclusion principle :-



- 129.** Which of the following configuration follows the Hund's rule :-



- 130.** The basis of three unpaired electrons present in the configuration of nitrogen is :-

- (1) Aufbau principle (2) Pauli's principle  
 (3) Hund's principle (4) Uncertainty principle

- 131.** The orbital with maximum energy is :-

- (1) 3d (2) 5p (3) 4s (4) 6d

- 132.**  $n$  and  $\ell$  values of an orbital 'A' are 3 and 2 and for another orbital 'B' are 5 and 0. The energy of :-

- (1) B is more than A  
 (2) A is more than B  
 (3) A and B are of same energy  
 (4) None

- 133.** No. of all subshells of  $n + \ell = 7$  is:-

- (1) 4 (2) 5 (3) 6 (4) 7

- 134.** Electronic configuration  $\uparrow\downarrow \uparrow\downarrow \uparrow\downarrow \uparrow\downarrow \square$  has violated :-

- (1) Hund's rule (2) Pauli's principle  
 (3) Aufbau principle (4)  $(n + \ell)$  rule

- 135.** The total spin resulting from a  $d^9$  configuration is:-

- (1)  $\frac{1}{2}$  (2) 2 (3) 1 (4)  $\frac{3}{2}$

- 136.** Which of the following transition neither shows absorption nor emission of energy in case of hydrogen atom :-

- (1)  $3p_x \rightarrow 3s$  (2)  $3d_{xy} \rightarrow 3d_{yz}$   
 (3)  $3s \rightarrow 3d_{xy}$  (4) All the above

- 137.** In ground state of  ${}_{24}\text{Cr}$ , number of orbitals with paired and unpaired electron :-

- (1) 10 (2) 12 (3) 15 (4) 18

- 138.** For Na ( $Z = 11$ ) set of quantum numbers for last electron is:-

- (1)  $n = 3, \ell = 1, m = 1, s = +\frac{1}{2}$   
 (2)  $n = 3, \ell = 0, m = 0, s = +\frac{1}{2}$   
 (3)  $n = 3, \ell = 0, m = 1, s = +\frac{1}{2}$   
 (4)  $n = 3, \ell = 1, m = 1, s = -\frac{1}{2}$

- 139.** Which of the following set of quantum numbers is correct for the 19<sup>th</sup> electron of Chromium :-

$n$	$\ell$	$m$	$s$
(1) 3	0	0	$1/2$
(2) 3	2	-2	$1/2$
(3) 4	0	0	$1/2$
(4) 4	1	-1	$1/2$

- 140.** Which set of quantum number is correct for an electron in 3p orbital :-

- (1)  $n = 3, \ell = 2, m = 0, s = +\frac{1}{2}$   
 (2)  $n = 3, \ell = 0, m = +1, S = +\frac{1}{2}$   
 (3)  $n = 3, \ell = -2, m = -1, s = +\frac{1}{2}$   
 (4)  $n = 3, \ell = 1, m = 0, s = +\frac{1}{2}$

- 141.** An atom of Cr [ $Z = 24$ ] loses 2 electrons. How many unpaired electrons shall be there in  $\text{Cr}^{+2}$ :

- (1) 4 (2) 3 (3) 2 (4) 1

- 142.** The atomic weight of an element is double its atomic number. If there are three electrons in 2p sub-shell, the element is :-

- (1) C (2) N (3) O (4) Ca

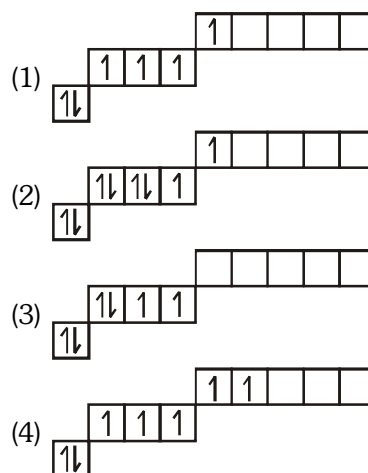
- 143.** The atomic number of an element is 17, the number of orbitals containing electron pairs in the valence shell is:-

- (1) 8 (2) 2 (3) 3 (4) 6



- 144.** A transition metal 'X' has a configuration  $[\text{Ar}] 3d^5$  in its + 3 oxidation state. Its atomic number is:-  
 (1) 22 (2) 26 (3) 28 (4) 19
- 145.**  $4s^2$  is the configuration of the outermost orbit of an element. Its atomic number would be :-  
 (1) 29 (2) 24 (3) 30 (4) 19
- 146.** Sum of the paired electrons present in the orbital with  $\ell = 2$  in all the species  $\text{Fe}^{2+}$ ,  $\text{Co}^{2+}$  and  $\text{Ni}^{+2}$  are:-  
 (1) 9 (2) 12 (3) 6 (4) 15
- 147.** What is the electronic configuration of an element in its first excited state which is isoelectronic with  $\text{O}_2$   
 (1)  $[\text{Ne}] 3s^2 3p^3 3d^1$  (2)  $[\text{Ne}] 3s^2 3p^4$   
 (3)  $[\text{Ne}] 3s^1 3p^3 3d^2$  (4)  $[\text{Ne}] 3s^1 3p^5$
- 148.** The quantum number of 20th electron of  $\text{Fe}(Z = 26)$  would be :-  
 (1) 3, 2, -2,  $-\frac{1}{2}$  (2) 3, 2, 0,  $\frac{1}{2}$   
 (3) 4, 0, 0,  $+\frac{1}{2}$  (4) 4, 1, -1,  $+\frac{1}{2}$
- 149.** The atomic number of the element having maximum number of unpaired 3p electrons is (in ground state):-  
 (1) 15 (2) 10 (3) 12 (4) 8

**150.** Which one represent ground state configuration :-



- 151.** The electronic configuration of a dipositive metal ion  $\text{M}^{2+}$  is 2, 8, 14 and its ionic weight is 58 a.m.u. The number of neutrons in its nucleus would be :-  
 (1) 30 (2) 32 (3) 34 (4) 42
- 152.** In an atom having 2K, 8L, 8M and 2N electrons, the number of electrons with  $m = 0$ ;  $s = +\frac{1}{2}$  are :-  
 (1) 6 (2) 2 (3) 8 (4) 16
- 153.** The number of electrons in the M-shell of the element with atomic number 24 is :-  
 (1) 24 (2) 12 (3) 8 (4) 13

### EXERCISE-I (Conceptual Questions)

### ANSWER KEY

Que.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans.	3	1	1	3	2	2	4	1	3	2	2	1	3	4	3
Que.	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
Ans.	3	3	1	3	3	4	3	4	1	3	1	1	3	2	4
Que.	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45
Ans.	4	4	1	1	2	1	4	1	3	3	1	4	1	1	4
Que.	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60
Ans.	1	2	4	4	4	3	1	1	2	1	3	1	3	4	4
Que.	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75
Ans.	1	1	2	4	1	3	4	3	4	1	2	4	2	1	2
Que.	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90
Ans.	3	3	2	1	4	1	3	3	1	4	1	1	3	2	3
Que.	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105
Ans.	1	1	1	2	1	1	3	4	1	4	4	1	4	1	3
Que.	106	107	108	109	110	111	112	113	114	115	116	117	118	119	120
Ans.	2	1	3	1	4	1	2	1	3	3	4	1	2	2	3
Que.	121	122	123	124	125	126	127	128	129	130	131	132	133	134	135
Ans.	4	3	2	3	3	4	4	2	1	3	4	1	1	1	1
Que.	136	137	138	139	140	141	142	143	144	145	146	147	148	149	150
Ans.	4	3	2	3	4	1	2	3	2	3	2	1	3	1	3
Que.	151	152	153												
Ans.	2	1	4												



## Directions for Assertion &amp; Reason questions

These questions consist of two statements each, printed as Assertion and Reason. While answering these Questions you are required to choose any one of the following four responses.

- (A) If both Assertion & Reason are True & the Reason is a correct explanation of the Assertion.  
 (B) If both Assertion & Reason are True but Reason is not a correct explanation of the Assertion.  
 (C) If Assertion is True but the Reason is False.  
 (D) If both Assertion & Reason are false.

- Assertion :-** In Rutherford's gold foil experiment, very few  $\alpha$ -particles are deflected back.  
**Reason :-** Nucleus present inside the atom is heavy.  
 (1) A (2) B (3) C (4) D
- Assertion :-** Mass numbers of most of the elements are fractional.  
**Reason :-** Mass numbers are obtained by comparing with the mass number of carbon taken as 12.  
 (1) A (2) B (3) C (4) D
- Assertion :-** In an atom, the velocity of electron in the higher orbits keeps on decreasing.  
**Reason :-** Velocity of electron is inversely proportional to radius of the orbit.  
 (1) A (2) B (3) C (4) D
- Assertion :-** Total energy of electron in hydrogen atom is negative.  
**Reason :-** It is in bound state.  
 (1) A (2) B (3) C (4) D
- Assertion :-** Limiting line in the Balmer series has a wavelength of 364.7 nm.  
**Reason :-** Limiting line is obtained for a jump of electron from  $n=\infty$  to  $n=2$  for Balmer series.  
 (1) A (2) B (3) C (4) D
- Assertion :-** A spectral line will be seen for a  $2p_x - 2p_y$  transition.  
**Reason :-** Only Balmer lines are observed in the visible region.  
 (1) A (2) B (3) C (4) D
- Assertion :-** Bohr model is not suitable in case of multielectron species.  
**Reason :-** It does not tell about electron-electron interaction.  
 (1) A (2) B (3) C (4) D
- Assertion :-** p-orbital has dumbbell shape.  
**Reason :-** Electrons present in p-orbital can have one of three values for 'm', i.e. 0, +1, -1  
 (1) A (2) B (3) C (4) D
- Assertion :-** Nodal plane of  $p_x$  atomic orbital is yz plane.  
**Reason :-** In  $p_x$  atomic orbital, electron density is zero in the yz plane.  
 (1) A (2) B (3) C (4) D
- Assertion :-** 2p orbitals do not have spherical nodes.  
**Reason :-** The number of spherical nodes in p-orbitals is given by  $(n-2)$ .  
 (1) A (2) B (3) C (4) D
- Assertion :-** There are two spherical nodes in 3s-orbital.  
**Reason :-** There is no angular node in 3s-orbital.  
 (1) A (2) B (3) C (4) D
- Assertion :-** Number of radial and angular node for 3p-orbital are 1, 1 respectively.  
**Reason :-** No. of radial and angular node depends only on principal quantum no.  
 (1) A (2) B (3) C (4) D
- Assertion :-** For hydrogen 2s & 2p have same energy.  
**Reason :-** For an atom, for same principal quantum number s, p, d & f have same energy.  
 (1) A (2) B (3) C (4) D
- Assertion :-** No two electrons in an atom can have the same values of four quantum numbers.  
**Reason :-** No two electrons in an atom can be simultaneously in the same shell, same subshell, same orbitals and have same spin.  
 (1) A (2) B (3) C (4) D



**15. Assertion :-** An orbital cannot have more than two electrons.

**Reason :-** The two electrons with opposite spin in an orbital create opposite magnetic field.

(1) A (2) B (3) C (4) D

**16. Assertion :-** In hydrogen energy of 4s is more than 3d.

**Reason :-** An orbital with lower value of  $(n+l)$  has smaller energy than the orbital with higher value of  $(n+l)$ .

(1) A (2) B (3) C (4) D

**17. Assertion :-** The configuration of B atom cannot be  $1s^2 2s^3$ .

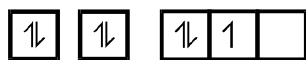
**Reason :-** Hund's rule demands that the configuration should display maximum multiplicity.

(1) A (2) B (3) C (4) D

**18. Assertion :-** The electronic configuration of nitrogen atom is represented as :



1s 2s 2p  
not as



1s 2s 2p

**Reason :-** The configuration of ground state of an atom is the one which has the greatest multiplicity.

(1) A (2) B (3) C (4) D

**19. Assertion :-** The ground state configuration of Cr is  $3d^5 4s^1$ .

**Reason :-** A set of exactly half filled orbitals containing parallel spin arrangement provide extra stability.

(1) A (2) B (3) C (4) D

**20. Assertion :-** When we give electron beam of 10.60 eV energy on hydrogen sample it will excite to first excited state.

**Reason :-** The difference between  $n_2$  and  $n_1$  is 10.2005 eV only.

(1) A (2) B (3) C (4) D

**21. Assertion :-** Bohr's model is not applicable for He atom.

**Reason :-** Bohr's theory does not consider inter electronic repulsion.

(1) A (2) B (3) C (4) D

**22. Assertion :-** Probability of finding an electron is directly proportional to wave function.

**Reason :-** In Bohr orbit revolving electron makes same number of waves.

(1) A (2) B (3) C (4) D

**23. Assertion :-** Heisenberg uncertainty principle is not applicable for a moving tennis ball.

**Reason :-** Tennis ball in motion does not exhibit wave nature.

(1) A (2) B (3) C (4) D

## EXERCISE-II(Assertion & Reason)

## ANSWER KEY

Que.	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Ans.	2	4	3	1	1	4	1	2	1	1	2	3	3	1	2
Que.	16	17	18	19	20	21	22	23							
Ans.	2	2	1	1	2	1	4	3							

